# Final Report of the $\bar{P} A N D A$ PID TAG 

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## 1 Introduction

The PANDA ([1]) PID TAG (Particle Identification Technical Assessment Group) was installed to give to the collaboration a complete set of parameters for an optimal set of particle detectors. The task given to this TAG is described in more detail:

Subject<br>- Requirements from physics<br>- Evaluate potential of each subsystem<br>- Matching of systems<br>\section*{Deliverables}<br>- Definition of global PID scheme<br>- Optimized set of detectors and parameters

This list reflects roughly the structure of the PID TAG work and of this report. In an additional subsection the tools available for the PID TAG work are presented and explained (see also [2]) . The PID TAG evaluated the necessity of mapping the "Separation Power" in dependence of the momentum and the polar angle of the reaction products which is described in section ??. Since a "full simulation" was not available to calculate the performance of all the sub detectors, the TAG gathered parameterizations of the single sub detectors which went into a "Fast Simulation" explained in section 4.3. For single physics channels a "Full Simulation" was used.

Amongst others some important questions to solve were:

- PID with and with out the information of a Time Projection Chamber (TPC)
- PID with and with out an Forward Endcap Cherenkov, and with different forms (Focusing Disc DIRC, Time of Propagation Disc DIRC and Proximity RICH)
- PID with and with out a Forward RICH

The PID TAG had about 10 presence meetings and over 15 on line meetings. First PID subsystems were defined. Each subsystem has its responsible representative. Each representative had a replacement of his own group to guarantee always the same level of knowledge in all subsystems. For special subjects experts were asked to present informations in the meeting or to give answers to questions which arose.

The members of the TAG and their special responsibilities are listed at the end of the document (section 9).

## 2 Physics Requirements

The HESR (High Energy Storage Ring) of the new FAIR (Facility for Antiproton and Ion Research) project provides an Antiproton beam of high resolution (down to $\Delta p=1 \times 10^{-5}$ ) and intensity from $1.5 \mathrm{GeV} / c$ to $15 \mathrm{GeV} / c$ momentum.
This offers the unique possibility of investigating a broad filed of physics. The vast variety of reaction types from meson-production over Charmonium decays to Hyper nuclear reactions demands a complete and compact detector system.

The physics requirements to the detectors are:

- to cover the full angular range of the physics products
- to detect all momenta of the reaction products
- to separate particle types with a defined level of separation over the full range of momenta of the reaction products.

The full solid angle can only be covered by the full set of detectors. Sometimes the momentum coverage has to be fulfilled by a combination of two or even three sub detectors.

For the single subsystems benchmark-channels had to be identified (Table 1) and simulated.

| Channel | Final state | Related to detector |
| :--- | :--- | :--- |
| $\bar{p} p \rightarrow(n) \pi^{+} \pi^{-}$ | $(n) \pi^{+} \pi^{-}$ | EMC |
| $\bar{p} p \rightarrow \psi(3770) \rightarrow D^{+} D^{-}$ | $2 K 4 \pi$ | DIRCs, ToF |
| $\bar{p} p \rightarrow \eta_{c} \rightarrow \phi \phi$ | 4 K | DIRCs |
| $\bar{p} p \rightarrow D_{S} D_{S 0}^{*}(2317)$ | $\pi^{ \pm} K^{+} K^{-}$ | DIRCs |
|  |  | muon |
|  |  | Forward RICH |

Table 1: Benchmark channels to evaluate the performance of the different PID detectors.

At $\overline{\text { PANDA }} 2 \times 10^{7}$ reactions per second with up to 10 charged particles per reaction have to be digested by the detectors.

## 3 PID Subsystems

The different behavior of charged particles traversing active and passive detector material can be used to identify (on a probabilistic level) the nature of a charged particle. The PID detectors used in PANDA take advantage of the following effects:

- Specific Energy Loss. The mean energy loss of charged particles per unit length, usually referred to as $\mathrm{dE} / \mathrm{dx}$, is described by the Bethe-Bloch equation which depends on the velocity rather than momentum of the charged particle.
- Cherenkov Effect. Charged particles in a medium with refractive index $n$ propagating with velocity $\beta>1 / n$ emit radiation at an angle $\Theta_{C}=\arccos (1 / n \beta)$. Thus, the mass of the detected particle can be determined by combining the velocity information determined from $\Theta_{C}$ with momentum information from the tracking detectors.
- Time-of-flight. Particles with the same momentum, but different masses travel with different velocities, thus reaching a time-of-flight counter at different times relative to a common start.
- Absorption. A thick layer of passive material absorb most particles due to electromagnetic (e+e-, $\gamma$ ) or hadronic interactions (all charged and neutral hadrons). After a certain amount of material only muons and neutrinos survive. The muons can then be detected easily with any kind of charged particle detector, depending on the desired speed and resolution.

The group of subsystems building the particle identification system of $\overline{\mathrm{P}} \mathrm{ANDA}$ are listed with growing distance to the Target point:

- Time Projection Chamber
- Time of Flight
- Barrel DIRC
- Barrel Calorimeter
- Forward Cherenkov
- Forward Calorimeter
- Muon Counter


### 3.1 Central Tracker



Figure 1: GEM-TPC working principle

### 3.1.1 Time Projection Chamber (TPC)

The TPC is discussed as a solution for the outer tracking within the target spectrometer (as Central Tracker). The required momentum resolution is $\approx 1 \%$, the required vertex resolution $\approx 150 \mathrm{um}$ in the xy plane and $<1 \mathrm{~cm}$ in z direction.

In addition provides the TPC in the momentum range below $\approx 1 \mathrm{GeV} / \mathrm{c}$ and above $\approx 2 \mathrm{GeV} / \mathrm{c}$ information for particle identification within the target spectrometer. Especially for particles with momenta below $\approx 1 \mathrm{GeV} / \mathrm{c}$ this is of great help for the overall PID performance and to supplement the information from the barrel DIRC.

Working principle
General:3D tracking device - charged particles ionize detector gas - electric field along cylinder axis separates positive gas ions from electrons - primary electrons drift towards readout anode gas amplification done by several GEM foils - ungated, continuous operation mode due to HESR beam properties - intrinsic ion feedback suppression by GEM foils - continuous data readout within PANDA DAQ - parallel online data reduction and processing (including tracking)
PID: performed via measurement of mean energy loss per track length (dE/dx), described by Bethe-Bloch-formula, in combination with (obligatory) momentum measurement - PANDA TPC offers to do $\approx 50-100$ (fluctuating) energy loss measurements per track - truncated mean algorithm used to get rid off Landau tail and to calculate mean.
Important values
Geometry: inner radius: 15 cm , outer radius: 42 cm , length: 150 cm , gas volume: 7001,2 separate chambers (due to target pipe)
Material budget: $\frac{X}{X_{0}} \approx 1.5 \%$
Detector gas: Ne/CO2 (90/10, maybe admixture of CH4), gas gain: several 1000
Operation: drift field: $400 \mathrm{~V} / \mathrm{cm}, 2 \mathrm{x} 2 \mathrm{~mm}$ pads (100000)
First estimates and simulations (obtained from old PANDA framework and preliminary)
Data were generated based on an event generator which shoots p, K, pi, mu and e (plus antiparticles) isotropically through the TPC. All tracks come from the IP, with momenta between 0.2 and $4 \mathrm{GeV} / \mathrm{c}$. Tracks are divided into 6 mm pieces, for each the energy loss is calculated resulting


Figure 2: Energy loss in the TPC vs. momentum


Figure 3: Energy loss resolution TPC
in 50-100 measurements depending on track length. Upper $40 \%$ are discarded and mean $\mathrm{dE} / \mathrm{dx}$ calculated (truncated mean). The spread of the these $\mathrm{dE} / \mathrm{dx}$ values for certain p bins is fitted with a Gaussian and the $\mathrm{dE} / \mathrm{dx}$ resolution is defined as the corresponding sigma.

The separation power between two particles is defined as:

$$
\begin{equation*}
\sigma_{\text {sep }}=\frac{2 *\left|I_{1}-I_{2}\right|}{\left(\frac{\sigma\left(I_{1}\right)}{I_{1}}+\frac{\sigma\left(I_{2}\right)}{I_{2}}\right)} \tag{1}
\end{equation*}
$$

where I stands for the $\mathrm{dE} / \mathrm{dx}$ of the respective particle. A constant $\mathrm{dE} / \mathrm{dx}$ resolution of $5 \%$ was assumed.

Note:For all the simulation results shown here the gas density value was a factor of 1.5 to high. Therefore we expect the performance to be a bit worse. For example the $\mathrm{dE} / \mathrm{dx}$ resolution will change from $5 \%$ to $7 \%$. Simulations will be repeated with the new PANDA framework as soon as possible.


Figure 4: TPC separation power vs. momentum
3.1.2 Straw Tube Tracker (STT)

### 3.2 Time of Flight (ToF)

### 3.3 Barrel DIRC

The purpose of the Barrel DIRC (Detection of Internal Reflected Cherenkov photons) is to provide a particle identification. The mass of the particle can be achieved by combining the velocity information of the DIRC with momentum information from the tracking detectors. In addition the distinction between gammas and relativistic charged particles entering the EMC behind the DIRC is possible.
Basis for the calculations and simulations are the bar dimensions taken from the BaBar DIRC [3]. With the length adapted to the $\overline{\mathrm{P}}$ ANDA setup there are quartz bars of $17 \times 35 \times 2300 \mathrm{~mm}^{3}$ and a distance of 480 mm to the target point. Thus the barrel DIRC covers the solid angle between 22 and 140 degrees. The lower momentum threshold for kaons which produce Cherenkov light is for an envisaged refractive index of $n=1.47$ as low as $460 \mathrm{MeV} / \mathrm{c}$ for single photon production. For larger photon numbers the threshold increases.
With 17 mm (of thickness) of fused silica the DIRC bars present approximately $14 \%$ of a radiation length to normal incident particles. The support structure will add $3 \%$.
This design is initially based on the BaBar DIRC [3] but at PANDA further improvements of the performance are under development. The combination of the spatial image of the photons with their time of arrival gives access not only to their velocity but also to the wavelength of the photons. Thus dispersion correction at the lower and upper detection threshold becomes possible. Further on the reduction of the photon readout in size and number of photon detectors is envisaged. A lens or a set of lenses at the exit of the quartz bar focus the photons to a focal plane behind a readout volume of about 30 cm length. When this volume is filled with a medium with the same refractive index as the radiator material $\left(\mathrm{n}_{\text {medium }}=\mathrm{n}_{\text {radiator }}=1.5\right)$ additional dispersion effects and other image distortions are avoided.
3.4 Barrel Calorimeter

### 3.5 Forward Cherenkov

Two DIRC design options exist for the endcap part of the target spectrometer section. These differ in the photon readout design but both use an amorphous fused silica radiator disc. The endcap detector position covers forward angles of up to $\vartheta=22^{\circ}$ excluding an inner rectangular (is it now elliptical??) area of $\vartheta_{x}=10^{\circ}$ horizontal and $\vartheta_{y}=5^{\circ}$ vertical half-angles. Simulations using the DPM generator [4] give $1.0 \pm 0.8$ (at $2 \mathrm{GeV} / \mathrm{c}$ ) to $2.3 \pm 1.8$ (at $15 \mathrm{GeV} / \mathrm{c}$ ) charged particle multiplicity per $\bar{p} p$ interaction emitted from the target vertex into this acceptance.

In such a one-dimensional ${ }^{1}$ DIRC type, a photon is transported to the edge of a circular disc while preserving the angle information. Avoiding too much light scattering loss at the surface reflections requires locally (in the order of millimeters) a surface roughness not exceeding several nanometers RMS.

The lower velocity threshold, which is common to both designs, depends on the onset of total internal reflection for a part of the photons emitted in the Cherenkov cone.
There are several boundary conditions for the disc thickness. Radiation length considerations as the detector is upstream of the endcap EMC call for a thin disc. The focussing design is workable with a 10 mm thickness $\left(X_{0}=126 \mathrm{~mm}\right)$. Regarding the mechanical stability and handling during polishing, current company feedback recommends 20 mm minimum thickness. The resulting thickness of the radiator disc has to be a compromise.

[^0]
### 3.5.1 Focussing Disc DIRC

In the Focussing Light guide Dispersion-Correcting design (Figures 5 and 6), when a photon arrives at the edge of the circular or polygonal disc, it enters into one of about hundred optical elements on the rim. Here the two-fold angular ambiguity (up-down) is lifted, the chromatic dispersion corrected and the photon focused onto a readout plane. While the optical element entered determines the $\phi$ coordinate, measuring the position in the dispersive direction on the focal plane of the focussing light guide yields the $\theta$ coordinate.


Figure 5: Polygonal disc with focussing light guides attached to the rim used as optical readout components.

Lithium fluoride ( LiF ) is UV transparent and has particularly low dispersion. Proton beam irradiation of a test sample shows that radiation-produced color centers are confined to sufficiently small wavelength ranges, and are only partially absorbing at the expected $\bar{P} A N D A$ lifetime dose. Hence we believe we can use LiF as a prism element (see Fig. 6) to correct the Cherenkov radiation


Figure 6: Light guide side view shown with a set of rays used for optimising the light guide curvature. Reflections at the parallel front and back surfaces keep the light inside but do not affect the focussing properties.


Figure 7: Simulated photon hit pattern for four particles emitted at different angles $\theta$ and $\phi$ from the target vertex.


Figure 8: Simulation-derived pion-kaon separation power for a focussing lightguide design with a 15 mm thick amorphous fused silica disc and 0.4 eV photon detection efficiency. Calculation February 2008.
dispersion. The two boundary surfaces, with the radiator disc and the subsequent light guide, make the chromatic dispersion correction angle-independent to first order.
As with the radiator, the light impinging on the inside of the light guide's curved surface undergoes total internal reflection, hence no mirror coating is needed. This reflection makes the focussing also independent of the wavelength.

With the light staying within the dense optical material of the light guide, most of the incoming light phase space from the disc is mapped onto the focal plane with its one-coordinate readout. The focussing surface with cylindrical shape of varying curvature has been optimised to give an overall minimum for the focus spot sizes of the different angles on the focal plane, individual standard deviations being well below 1 mm for the instrumented area.

For an Endcap DIRC detector with 128 lightguides and 4096 detector pixels that fits inside the target spectrometer return yoke, Figure 8 shows the angle-dependent upper momentum limit being about $4-6 \mathrm{GeV} / \mathrm{c}$ for $4 \sigma$ pion-kaon separation within the acceptance $\vartheta=5^{\circ}-22^{\circ}$.
Typically all of the 40 detected photons per particle arrive within a 4 ns time window.
Each lightguide can individually be assigned its own 0.4 ns acceptance window. For the pixel size used in this simulation they are contained inside a 40 pixel•ns volume, which at 4 K detector pixels amounts to 10 ps detector occupancy time per particle signature.

222 The detected photon rate (source: presentation KF 2007-03-27 Genova, 2E7 interactions; scaled ${ }_{223}$ to 4 K pixels) is $3 \mathrm{E} 7 \mathrm{~s}^{-1}$ per PMT and 1E6 $s^{-1}$ per detector pixel.


Figure 9: Sketch of the flightpath in the ToP Disc

### 3.5.2 Time of Propagation Disc DIRC

In the Multi-Chromatic Time-of-Propagation design ([5]) small detectors measure the arrival time of photons on the disc rim, requiring $\sigma_{t}=30-50 \mathrm{ps}$ single photon time resolution. For any given wavelength, the disc edge is effectively covered alternately with mirrors and detectors. Only due to the resulting different light path-lengths one can determine accurately enough the start reference time, i.e. the time when the initial charged particle enters the radiator, as the stored anti proton beam in the HESR has no suitable time structure to be used as an external time start.

As some of the light is reflected several times before hitting a detector, the longer path lengths allow a better relative time resolution.

The use of dicroic mirrors as color filters allows the use of multiple wavelength bands within the same radiator (the current design suggesting two bands) resulting in higher photon statistics. The narrow wavelength bands minimise the dispersion effects, and the quantum efficiency curve of the photo cathode material could be optimised for each wavelength band individually.

### 3.5.3 Proximity RICH

As alternative approaches Proximity Imaging Solutions were considered.

- Liquid radiator proximity RICH using CsI GEMs: Proximity focusing RICH detectors use the most simplest imaging geometry. Their resolution depends on the optical quality and crucially on the ratio of radiator thickness to stand-off distance, the distance between the creation and detection of the photon. Using liquid or solid radiators yielding enough Cherenkov photons, the radiator can be kept rather slim, which in turn only require moderate stand-off distances on the order of 100 mm . The ALICE HMPID detector is build in this fashion using a C6F14 liquid radiator and CsI-photon cathodes in an MWPC. This requires a UV optic. It is proposed to use the same radiator technique and combine the third tracking station with a CsI coated GEM photon detector. The detector will be thicker along the beam direction than the DIRC detector previously described, but can be essentially moved to any position along the beam axis. The estimated performance and the ALICE/STAR test results show a significant decrease in performance compared to the DIRC solutions.
- Solid radiator proximity RICH using CsI GEMs: One of the main drawbacks of using the ALICE design is the use of C6F14. This radiator is rather sensitive to impurities and radiation damage requiring a purification system. Using a fused silica disc with a properly machined surface as radiator circumvents the problem while keeping the geometrical advantages of the design. Initial studies show a further reduction of performance mainly due to strong dispersive effects in the UV region.
- Aerogel proximity RICH using PMTs: The Belle endcap Cherenkov threshold counter will be replaced by a proximity imaging RICH counter using an Aerogel radiator and conventional BiAlkali based multi-pixel PMTs as photon detectors. Using a so-called focusing radiator scheme, prototypes show excellent performances. The main technological challenge for this detector is to realise a photon detection matrix in a strong magnetic field. Recent developments in the field of proximity focusing HAPDs seem to make such a detector realistic. The large number of pixels required should the detector be placed behind the EMC, but inside the cryostat merit a detailed look at the costs of such a design.
3.5.4 Forward RICH

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### 3.6 Forward Calorimeter

3.7 Muon Counter

## 4 Tools

In this section the TAG work is described. To evaluate the performance of the detectors the PID TAG defined the "Separation Power" as the right tool (see section ??. With the help "Phase Space Plots" (section 4.2) the angular coverage and the coresponding particle momenta could be determined. The "Fast Simulation" (section 4.3) was used to map the separation power over the full angular and momentum range. In a second step important reactions and their relevant background channels were simulated. Thus the regions where a good separation power is needed could be identified and checked whether the detector performance is sufficient there.

### 4.1 Separation Power

This document completely deals with the quality of the particle identification of the projected PANDA detector. Thus the major issue upon which decisions can be made is a proper definition of classification quality or performance.

The according concept chosen for that purpose called 'Separation Power' bases on the assumption that the particular observables of objects of different classes exhibit more or less gaussian distributions.

Consider the situation illustrated in fig. 10.


Figure 10: Illustration for the definition of separation power.

There are plotted two gaussian distributions $G_{1}(x) \equiv G\left(x ; \mu_{1}, \sigma_{1}\right)$ and $G_{2}(x) \equiv G\left(x ; \mu_{2}, \sigma_{2}\right)$ with mean values $\mu_{1}=1.5$ and $\mu_{2}=3.5$ and standard deviations $\sigma_{1}=0.25$ and $\sigma_{2}=0.5$. This could be e. g. the probability density distributions of the $d E / d x$ measurements for two particle species in a small momentum range. Obviously the distributions are separable quite reasonable, but what is the measure for the separation potential?

A proper definition would be to define a particular classificator, e.g. every particle with property $x_{0}<2$ is considered as member of class 1 (red). Then one can determine two quantities which are of relevance for the qualtity of classification. The first one ist the efficiency, which is part of the distribution 1 (or a random sample of measurements following this distribution) which is identified correctly analytically corresponding to the integral

$$
\begin{equation*}
\epsilon=\int_{-\infty}^{x_{0}} G_{1}(x) d x \tag{2}
\end{equation*}
$$

for a normalized Gaussian. The second quantity is the misidentification level given by the integral

$$
\begin{equation*}
\operatorname{mis-id}=\int_{-\infty}^{x_{0}} G_{2}(x) d x \tag{3}
\end{equation*}
$$

1. These two values would define clearly the performance of the classificator ${ }^{2}$. But this solution cannot be applied in case when one does not want to define a particular selector. It rather has to be defined a measure for the prospective performance of a possible selector.

Exactly this is the aim of the separation power $N_{\sigma}$ which relates the distance of the mean values $d=\left|\mu_{1}-\mu_{2}\right|$ of the two distributions to their standard deviations $\sigma_{1}$ and $\sigma_{2}$. The usual unit of $N_{\sigma}$ is 'number of gaussian sigmas of the separation potential', which is supposed to relate the number with gaussian integral values.
There are actually a lot of different definitions for that quantity on the market but it has been found an agreement within the PID TAG on the following definition:

$$
\begin{equation*}
N_{\sigma}=\frac{\left|m_{1}-m_{2}\right|}{\sigma_{\beta}}=\frac{\left|m_{1}-m_{2}\right|}{\left(\sigma_{1} / 2+\sigma_{2} / 2\right)} \tag{4}
\end{equation*}
$$

This relationship is illustrated in fig. 10. The black dashed line marks the position $x_{0}$ between the two distributions, for which the differences to each mean value $\left|m_{1}-x_{0}\right|=N_{\sigma} \cdot \sigma_{1} / 2$ and $\left|m_{2}-x_{0}\right|=N_{\sigma} \cdot \sigma_{2} / 2$ are the same in terms of $\sigma$ 's.
This means a separation of e. g. $N_{\sigma}=4 \sigma$ corresponds to a gaussian integral

$$
\begin{equation*}
I=\int_{-\infty}^{\mu+4 \sigma / 2} G(x ; \mu, \sigma) d x=0.9772 \tag{5}
\end{equation*}
$$

which shall express an efficiency around $\epsilon \approx 97.7 \%$ or a mis-ID level around mis $=100 \%-97.7 \% \approx$ $2.3 \%$ or both. This integration up to half the number of sigmas $N_{\sigma} / 2$ seems a bit contra intuitive but is common notion and therefore has kept for the considerations in this document. Another feature of this definition is that it is symmetric for both classes or distributions, even with different $\sigma$ 's. Furthermore for the particular case of normalized gaussian distributions and a selector requiring $x<x_{0}$ for classifying class 1 objects in the upper example, the efficiency $\epsilon$ and purity $\pi$ for this selection have the same value, since

$$
\begin{align*}
\epsilon & =\frac{\int_{-\infty}^{x_{0}} G_{1}(x) d x}{\int_{-\infty}^{+\infty} G_{1}(x) d x}=\frac{\int_{-\infty}^{x_{0}} G_{1}(x) d x}{1}=\frac{\int_{-\infty}^{x_{0}} G_{1}(x) d x}{\int_{-\infty}^{x_{0}} G_{1}(x) d x+\int_{x_{0}}^{+\infty} G_{1}(x) d x}  \tag{6}\\
& =\frac{\int_{-\infty}^{x_{0}} G_{1}(x) d x}{\int_{-\infty}^{x_{0}} G_{1}(x) d x+\int_{-\infty}^{x_{0}} G_{2}(x) d x}=\frac{\int_{-\infty}^{x_{0}} G_{1}(x) d x}{\int_{-\infty}^{x_{0}} G_{1}(x)+G_{2}(x) d x}=\pi \tag{7}
\end{align*}
$$

Taking into account that quantities in reality never have gaussian shape the values $\sigma$ in fact are not necessarily gaussian sigmas but calculated as the root-mean-square (which actually is the standard deviation)

$$
\begin{equation*}
\sigma_{\mathrm{rms}}=\sqrt{\sum_{i}\left(x_{i}-\mu\right)^{2}} \tag{8}
\end{equation*}
$$

what in case of gaussian distribution would be indeed identical with the gaussian $\sigma$ from above. For the given example in fig. 10 the definition (4) computes to

$$
N_{\sigma, 1}=\frac{2}{0.25 / 2+0.5 / 2} \sigma=\frac{2}{0.375} \sigma=5.333 \sigma .
$$

[^1]
### 4.1.1 Mapping Separation Power

For the purpose of illustration the relationship between kinematic distributions of physics channels and the PID quality the separation power defined in (4) has been determined as 2-dimensional histogram in phase space $(p, \theta)$. Therefore it was necessary to computed the mean value $\mu$ and standard deviation $\sigma$ for every bin $i$ with $\left[p_{i} \ldots p_{i}+d p ; \theta_{i} \ldots \theta_{i}+d \theta\right]$ for bin widths $d p$ and $d \theta$ for every detector and particle species.
One technical remark: To avoid the computation of $(x-\mu)$ for every measurement in order to determine $\sigma$, which is very time consuming for large datasets, the relationship

$$
\begin{equation*}
\sigma=\frac{1}{N} \sqrt{\sum x_{i}^{2}-\left(\sum x_{i}\right)^{2}} \tag{9}
\end{equation*}
$$

has been exploited which does not require a previous calculation of the mean value $\mu=\bar{x}$.
In figs. 11 and 12 the combined separation power is presented for the detector setup comprising the PID relevant systems

- Micro Vertex Detector
- Barrel Time of Flight System
- Barrel DIRC
- Disc DIRC
- RICH
and either the Straw Tube Tracker (fig. 11) or the Time Projection Chamber (fig. 12) as central tracker option. The particle combinations investigated are

1. electron - muon (top left)
2. muon - pion (top right)
3. pion - kaon (middle left)
4. kaon - proton (middle right)
5. electron - pion (bottom left)

The results are determined based upon 5 million isotropic distributed single track events with particle momenta up to $6 \mathrm{GeV} / c$.
One should keep in mind that the conclusive power of separations involving electrons and muons is limited for the time being since no information from the electromagnetic calorimeters and the muon detectors has been incorporated so far, which have a significant impact on electron and muon identification respectively.


Figure 11: Combined map of Separation Power with STT as central tracker option. Color code corresponds to $N_{\sigma}=1 \ldots 8$.


Figure 12: Combined map of Separation Power with TPC as central tracker option. Color code corresponds to $N_{\sigma}=1 \ldots 8$.

### 4.2 Phase Space Plots

The question which has to be answered concerning particle identification is not only how good the classification works or has to work, but also in which region of the phase space one needs good separation, and in which parts one possibly doesn't need almost any.

Therefore it is a crucial task to visualize the kinematic behaviour of various important physics channels to get a better insight to the above issue. Furthermore not only kinematic distributions of signal events are relevant, since good PID is only useful in cases where kinematic overlap of particles of species $A$ from signal events and particles of species $B$ from background events really exists. In scenarios where particles of the same type $A$ appear in signal as well as background events in the same phase space location the background suppression cannot be improved by means of PID.

Following a request of the PID TAG phase space plots from all the reactions relevant for the physics book were produced. The set of plots shows for each particle species of the reaction the particle momentum versus theta angle.

| Signal Channel | Background channel | $E_{\text {cms }}[\mathrm{MeV}]$ | Fig. |
| :---: | :---: | :---: | :---: |
| $\bar{p} p \rightarrow J / \psi \pi^{+} \pi^{-}, J / \psi \rightarrow e^{+} e / \mu^{+} \mu^{-}$ | DPM | 4260 | - |
| $\bar{p} p \rightarrow D^{+} D^{-}, D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$ | DPM | 3750 | - |
| $\bar{p} p \rightarrow D^{0} \bar{D}^{0}, D^{0} \rightarrow K^{-} \pi^{+}$ | DPM | 3750 | - |
| $\bar{p} p \rightarrow D^{*+} D^{*-}, D^{*} \rightarrow D 0 \pi^{+} / D^{+} \pi^{0}$ | DPM | 4030 | - |
| $\bar{p} p \rightarrow D^{* 0} D^{* 0}$ | DPM | 4030 | - |
| $\bar{p} p \rightarrow Y(3940) \rightarrow J / \psi \omega, \omega \rightarrow \pi^{+} \pi^{-} \pi^{0}$ | DPM | 3940 | - |
| $\bar{p} p \rightarrow \bar{Y}(4320) \rightarrow \psi(2 S) \pi^{+} \pi^{-}, \psi(2 S) \rightarrow J / \psi \pi^{+} \pi^{-}$ | DPM | 4320 | - |
| $\bar{p} p \rightarrow D_{s}^{+} D_{s 0}^{*}(2317)^{-}, D_{s}^{+} \rightarrow \phi \pi^{+}$ | DPM | 4295 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | DPM | 2230 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | $\bar{p} p \rightarrow K^{+} K^{-} \pi^{+} \pi^{-}$ | 2230 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | $\bar{p} p \rightarrow \pi^{+} \pi^{-} \pi^{+} \pi^{-}$ | 2230 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | DPM | 5473 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | $\bar{p} p \rightarrow K^{+} K^{-} \pi^{+} \pi^{-}$ | 5473 | - |
| $\bar{p} p \rightarrow \phi \phi, \phi \rightarrow K^{+} K^{-}$ | $\bar{p} p \rightarrow \pi^{+} \pi^{-} \pi^{+} \pi^{-}$ | 5473 | - |

Table 2: Table of Phase Space Channels






Figure 13: Plot 1







Figure 14: Plot 2

### 4.3 Fast Simulation

In order to get information about phase space (i.e. momentum-polar angle dependence) coverage of the different PID relevant subsystems maps of separation power have been generated based on fast simulations of single track events, i.e. the particles properties are modified with an effective parametrization of detectors responses and PID information is estimated and attached to the resulting particle candidate. Since no microscopic simulation is performed and no exact geometry information is taken into account, the accuracy of this approach is limited, the computation time on the other hand is orders of magnitude shorter offering the possibility to do studies with higher statistics.

### 4.4 General Technique

In contrast to microscopic simulations using software systems like Geant or Fluka the Fast Simulation is based on acceptance filtering and effective parametrization of all observables of the particular subsystems. Underlying assumption is that the detector system will be able to recontruct the true particles properties like momentum, direction, energy, charge and particle identification (PID) information with uncertainties which are basically uncorrelated and can be described reasonable by parametric models. That could as simple example be gaussian uncertainty for momentum reconstruction with $\delta p / p=\sigma_{p}=2 \%$, which will be used to modify the true (i.e. generated) tracks parameters accordingly. Additionally a simple geometric accptance requirement will decide whether a track has been detected by a particular detector component or not.

There is a lot of freedom for the implementation of the subsystems, but a minimalistic detector description comprises

- Sensitivity information: Detects charged or neutral particles or both?
- Polar angle coverage: $\theta_{\text {min }}<\theta<\theta_{\text {min }}$
- Gaussian resolution of observables: $\sigma_{1}, \ldots, \sigma_{n}$

In order to apply these simulation scheme for every trackable particle coming from the event generator the following procedure is processed:

1. For all detectors $D_{j}, 1<j<m$

- In case $D_{j}$ detects the particle, collect resolution information for all measurable quantities.

2. When no detector detected the track, skip it.
3. Merge all resolution information; when e. g. the particle has been detected by $n$ devices capable of measuring momentum $p$ with resolutions $\sigma_{p, 1}, \ldots, \sigma_{p, n}$, the total resolution is

$$
\sigma_{p}=\left(\sum_{i=0}^{n} \frac{1}{\sigma_{p, i}^{2}}\right)^{-\frac{1}{2}}
$$

4. Modify the according quantities $x$ of the original track in the way $x^{\prime}=x+\delta x$, with $\delta x$ randomly chosen from gaussian distribution $G\left(\mu=0, \sigma_{x}\right)$
5. Create PID information according to the particles properties and attach to the particle; add particle to the track list
6. (Optional) Create secondary particles related to particles properties and add to the track list

With the so prepared track list analysis can be performed. The interface for doing that is exactly the same as the one for full simulated events.

Since this document is focussing on PID the relevant features will be describe in more detail in the following chapters. This will be done effect- or observable-wise instead of detector-wise, since the observed quantities

- specific energy loss $d E / d x$ (MVD, TPC, STT)
- Cherenkov angle $\theta_{C}$ (Barrel DIRC, Disc DIRC, RICH)
- reconstructed squared mass $m^{2}$ (TOF)
- EMC related measurements like $E_{\text {cluster }} / p$ or Zernike momenta.
govern the PID quality and performance and thus are a better ordering criterion. Unfortunately the latter information from calorimetry did not go into all results presented in this document due to technical reasons.


### 4.5 Tracking Detectors

Although not of direct impact to the field of PID the process of tracking delivers vital information for many of the PID relevant systems. Most of these like e.g. the Time-of-flight (TOF) system or Cherenkov devices (DIRCs and RICH) do not allow for performing a stand alone position measurement, thus their information have to be linked to tracks reconstructed by tracking devices. In addition for the purpose of evaluating PID likelihood functions one usually needs to compute expected values for observables like the Cherenkov angle $\theta_{C}$ or energy loss $d E / d x$ which will be computed for the reconstructed momentum value of the track. This certainly will differ from the true momentum value and therefore track reconstruction accuracy has important impact on likelihood based classification methods.

The approach for reconstruction of momenta in the Fast Simulation nevertheless is a very simple one assuming a global momentum resolution $\delta p / p$ for the track reconstruction, since due to technical reasons the particular detector components cannot exchange information. This implies that the tracking devices are not able to feed their information into the PID systems.

### 4.6 Energy Loss Parametrization

The computation of the specific energy loss is based on the Bethe-Bloch formula which very precisely takes into account the processes of charged particles interacting with matter. The formula and detailled information about parameter meanings in this term can be found in [6].

The expression looks quite complicated but can be evaluated straight forward with momentum $p$ and mass $m$ given as input. Additionally one has to substitude a lot of other, material related constants. Since we are not interested in the absolut energy loss but only in relative losses for different particle species it is not crucial to have very precise knowledge about the fixed parameters. In order to generate a simulated detector response for detectors capable of measuring $d E / d x$ a gaussian resolution $\sigma_{d E / d x}$ has been set for each of them. The simulated measured $(d E / d x)_{\text {sim }}$ value thus has been simply computed with formula (??) to

$$
\begin{equation*}
\left(\frac{d E}{d x}\right)_{\operatorname{sim}}=\left(\frac{d E}{d x}\right)+\delta\left(\frac{d E}{d x}\right) \tag{10}
\end{equation*}
$$

with randomly chosen value $\delta(d E / d x)$ from a gaussian distribution $G\left(\mu=0, \sigma_{d E / d x}\right)$.

### 4.7 Cherenkov Angle Parametrization

Basic theoretical information about the origin of Cherenkov radiation can be found elsewhere and will not be discuss here. The Cherenkov angle defined as the opening angle of the cone of radiation relativ to the direction of the incident charged particles momenta in medium with refractive index $n$ is given by the expression

$$
\begin{equation*}
\theta_{C}=\arccos \left(\frac{1}{\beta \cdot n}\right) \tag{11}
\end{equation*}
$$

with $\beta=p \cdot c / E$ being the velocity of the particle. Obviously computation of the expected Cherenkov angle for any given particle detected by the specific detector is straight forward. Key ingredient of the parametrization of the detector response is the resolution estimation. In case of DIRC detectors experience from the working device in the BaBar experiment tells us that the overall reconstruction resolution of the Cherenkov angle can be based on a single photon resolution $\sigma_{\text {s.phot. }} \approx 10 \mathrm{mrad}$. Responsible for the overall resolution then exclusively is the number of detected Cherenkov photons $N$ through

$$
\sigma_{\mathrm{tot}}=\frac{\sigma_{\mathrm{s.phot} .}}{\sqrt{N}}
$$

which is simple count statistics. This number $N$ has to be estimated and depends on

- the number of generated photons

$$
\begin{equation*}
N_{0}=2 \pi \cdot \alpha \cdot L\left(\frac{1}{\lambda_{\min }}-\frac{1}{\lambda_{\max }}\right) \cdot \sin ^{2} \theta_{C}=2 \pi \cdot \alpha \cdot L\left(\frac{1}{\lambda_{\min }}-\frac{1}{\lambda_{\max }}\right) \cdot\left(1-\frac{m^{2}+p^{2}}{p^{2} \cdot n^{2}}\right) \tag{12}
\end{equation*}
$$

with parameters

- fine structure constant $\alpha$
- trajectory length $L$ in the radiator material
- mass and momentum $m$ and $p$ of the incident track
- wave length region $\lambda_{\min }$ and $\lambda_{\max }$ where the photon detector is sensitive and
- refraction index $n$
- the trapping fraction $r_{\text {trap }}$ which is the fraction of the photons kept in the radiator/lightguide due to total reflection and
- the detection efficiency $\epsilon$ of the photon detector, e.g. a photo multiplier tube (PMT)

In order to derive the path length $L$ in the material one has to distinguish between the different Cherenkov devices.

In case of the Barrel DIRC on first of all has to compute the curvature due to the motion of a charged particle in a magnetic solinoidal field $B=B_{z}$. The radius $r$ of the circular shape in $(x, y)$ projection is given by

$$
\begin{equation*}
r=\frac{p_{t}}{q \cdot B}=\frac{3.3356 \cdot p_{t}[\mathrm{GeV} / c]}{B[\mathrm{~T}]} . \tag{13}
\end{equation*}
$$

for a particle with charge $q= \pm e$ and transverse momentum $p_{t}=p \cdot \sin \theta$. Based on this one can calculate the entering angle $\psi$ in $\phi$ direction to

$$
\begin{equation*}
\psi=\arccos \frac{r_{B}}{2 \cdot r} \tag{14}
\end{equation*}
$$

with $r_{B}$ being the radius of the DIRC Barrel i.e. the distance between the bars and the beam line. Here it is obvious that particles with $2 \cdot r<r_{B}$ will not hit the detector at all defining a minimum transverse momentum $p_{t, \min }$. The path length after some geometrical considerations then computes to

$$
\begin{equation*}
L \approx d_{\mathrm{bar}} \cdot \sqrt{\frac{1}{\sin ^{2} \theta}+\frac{1}{\tan ^{2} \psi}} \tag{15}
\end{equation*}
$$

where $d_{\mathrm{bar}}$ is the thinkness of the radiator bars and $\theta$ the dip angle of the helix of the track. The expression is an approximation because curvature within the bar has been neglected. This leads to significant wrong values for particles with $2 \cdot r \approx r_{B}$.
For the Disc DIRC and the RICH computing the radiator path length is much simpler. Here $L$ only depends on the dip angle and the radiator thinkness $d_{\text {rad }}$ resulting in

$$
\begin{equation*}
L=\frac{d_{\mathrm{rad}}}{\cos \theta} \tag{16}
\end{equation*}
$$

Also here no curvature within the radiators has been taken into account. This anyway would lead to more complicated estimates since angular changes along the radiator path results in systematic worsening of the Cherenkov angle which is neglected completely.
Finally we still need the trapping fraction $r_{\text {trap }}$ to determine the number of detected photons. There is no known analytic expression to compute this, thus 2 dimensional lookup tables $r_{\text {trap }}(\theta, p)$ for every particle species have been prepared. Figure 15 shows as an example the trapping fraction in the Barrel DIRC bars for muons and protons as a function of momentum $p$ and dip angle $\theta$.
With the path length $L$ one can evaluate expression (12) so that the detected number of photons can be estimated to

$$
\begin{equation*}
N=N_{0}^{\prime} \cdot \epsilon \cdot r_{\text {trap }} \tag{17}
\end{equation*}
$$

where the $N_{0}^{\prime}$ is randomly generated from Poisson distibution with input value $\lambda=N_{0}$. This directly leads to the expected resolution $\sigma_{\text {tot }}$ which is taken as the absolute uncertainty of the measurement of the Cherenkov angle. The simulated measured Cherenkov angle thus has been computed with formula (11) to

$$
\begin{equation*}
\theta_{C, \operatorname{sim}}=\theta_{C}+\delta \theta_{C} \tag{18}
\end{equation*}
$$

with randomly chosen value $\delta \theta_{C}$ from a gaussian distribution $G\left(\mu=0, \sigma_{\mathrm{tot}}\right)$.


Figure 15: 3-dimensional picture of the trapping fraction for protons in the Barrel DIRC (left) and the Disc DIRC as a function of momentum $p$ and dip angle $\theta$.

### 4.8 Time Of Flight Parametrization

From the geometrical point of view the calculation of the expected time of flight of a particle has similarities to the considerations done in 4.7 for the Barrel DIRC, since the TOF detector has also cylindrical shape. This requires also the particles with curvatures given by equation (13) to have a minimum transverse momentum $p_{t}$ to reach the detector and produce a signal.
In order to compute the time of flight $t_{\mathrm{TOF}}=s / v$ one in principal only needs the traveled distance $s$ and the velocity $v$ of the particle. While the latter one is simple to get by via the particles $\beta=p \cdot c / E$, the distance is not so easy to calculated due to the tracks curvature in the magnetic field. Nevertheless the calculation can be simplified exploiting the fact that the particles motion in $z$ direction is independent of that one in th $(x, y)$ plane. Therefore $t$ can also be calculated via the ratio of the travelled angle $\Phi$ and the angular velocity $\omega$

$$
\begin{equation*}
t_{\mathrm{TOF}}=\frac{\Phi}{\omega}=\frac{1}{\omega} \cdot 2 \arcsin \frac{r_{B}}{2 r} \tag{19}
\end{equation*}
$$

with the determination of $\Phi$ illustrated in fig. 16. The angular velocity in the projected plane is given by

$$
\begin{equation*}
\omega=\frac{B}{3.3356 \cdot E} \tag{20}
\end{equation*}
$$

for a magnetic field $B[\mathrm{~T}]$ and $E[\mathrm{GeV}]$. With these expressions one can derive the true expected time of flight. What now has to be simulated is the expected accuracy of the measurement achieved by the detector. This depends on the time resolution assumed to be $\sigma_{t} \approx 100 \mathrm{ps}$ on one hand and on the resolution connected to track reconstruction on the other hand since the transverse momentum $p_{t}=p \cdot \sin (\theta)$ is needed to compute the flight length. Only a relative uncertainty $\sigma_{p}=\delta p / p \approx 2 \%$ for the reconstructed absolute value of the momentum has been taken into account with respect to this, neglecting errors in polar angle measurement.

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Figure 16: Projection of particle trajectory to $(x, y)$ plane in order to determine $\Phi$.

This results in measured values

$$
\begin{align*}
t_{\mathrm{TOF}}^{\prime} & =t_{\mathrm{TOF}}+\delta t  \tag{21}\\
p^{\prime} & =p \cdot(1+\delta p) \tag{22}
\end{align*}
$$

with gaussian distributed deviations $\delta t$ and $\delta p$ according to $G\left(\mu=0, \sigma_{t}\right)$ and $G\left(\mu=0, \sigma_{p}\right)$. The primes denote from now the 'measured' or 'simulated' quantities. Now one basically has to reverse the process from above to get the simulated reconstructed value for the energy $E$ needed to compute the squared mass

$$
\begin{equation*}
m^{\prime 2}=E^{\prime 2}-p^{\prime 2} \tag{23}
\end{equation*}
$$

${ }_{518}$ which acts as the observable of the TOF detector. Starting point is eq. (20) which forms to like

$$
\begin{equation*}
m^{\prime 2}=\left(\frac{B \cdot t_{\mathrm{TOF}}^{\prime}}{2 \cdot 3.3356 \cdot \arcsin \left(\frac{r_{B}}{2 \cdot 3.3356 \cdot p^{\prime} \sin (\theta)}\right)}\right)^{2}-p^{\prime 2} \tag{24}
\end{equation*}
$$

## 5 Evaluation

5.1 Potential of the Subsystems

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5.2 Matching of the Subsystems

## 6 Global PID Scheme

The PANDA spectrometer will feature a complete set of innovative detectors for particle identification. The detection of neutral particles will be performed by a highly granular electromagnetic calorimeter. Charged particles will be identified in the low momentum region by their energy deposit and ToF, in all other momentum regions by innovative DIRC detectors. The target spectrometer will be complemented by a forward spectrometer to detect high momentum particles and surrounding muon detectors. Each detector systems performance is optimised in itself. Studies have begun to combine the responses of various detectors in a common framework based on a likelihood scheme or a carefully trained neutral network. These combined likelihood schemes are successfully employed at various detector systems like HERMEs, Belle and BaBar. They rely on a reliable parametrisation of the detector component response from simulation and test-beams. This has to be taken into account in testing PANDA's individual components. The combined performance of the system will be significantly better than the individual separation powers.

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7 Conclusion
${ }_{539}$ Thanks to analyzers from the " $\bar{P} A N D A$ Physics Book", and all who help with their work and 540 expertise to the success of the PID TAG.
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## 9 Appendix

Members of the PID TAG

- G. Schepers, C. Schwarz - Barrel Dirc (Chairs)
- B. Kopf, R. Novotny - Barrel Calorimeter
- B. Seitz - Cherenkov Counter (Global PID)
- O. Denisov / M. P. Bussa - Muon Counter
- K. Föhl / P. Vlasov - Forward Cherenkov
- J. Smyrski / O. Wronska - Forward Calorimeter
- Q. Weitzel / S. Neubert - Time Pjection Chamber
- C. Schwarz, A. Galoyan - Time of Flight
- K. Götzen - Fast Simulation
- K. Peters - Physics


[^0]:    ${ }^{1}$ Light is only reflected on surfaces of one spatial orientation, here the two disc surfaces both normal to the z axis.

[^1]:    ${ }^{2}$ For Bayes' classification a flux correction would have to be taken into account additionally. This requires of course knowledge about a posteriori probabilities of particle fluxes which not necessarily is available since significantly dependent on the given trigger and reaction type.

