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# Baryon Physics with PANDA

Karin Schönning, Uppsala University,  
on behalf of the Hyperon Physics Working Group, PANDA

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Uppsala, Sweden





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# Outline

- Introduction
- Part I: Baryon Spectroscopy
  - Baryons and the quark model
  - Light baryons
  - Strange hyperons
  - Prospects for PANDA
- Part II: Spin observables in  $\bar{p}p \rightarrow \bar{Y}Y$ 
  - Spin  $\frac{1}{2}$  hyperons
  - Spin  $\frac{2}{3}$  hyperons
  - CP violation
  - Previous measurements of  $\bar{p}p \rightarrow \bar{Y}Y$
  - Prospects for PANDA





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# Introduction

- Light quark ( $u, d$ ) systems:
  - Highly non-perturbative interactions.
  - Relevant degrees of freedom are hadrons.
- Systems with strangeness
  - Scale:  $m_s \approx 100 \text{ MeV} \sim \Lambda_{\text{QCD}} \approx 200 \text{ MeV}$ .
  - Relevant degrees of freedom unclear.
  - **Probes QCD in the intermediate domain.**
- Systems with charm
  - Scale:  $m_c \approx 1300 \text{ MeV}$ .
  - Quark and gluon degrees of freedom more relevant.
  - **By comparing strange and charmed hyperons we learn about QCD at two different energy scales.**



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# Why baryons?

## **Baryon Spectroscopy**

- New baryon states?
- Properties of already known states.
- Symmetries in the observed spectrum?



# Why baryons?

## **Baryon Spectroscopy**

- New baryon states?
- Properties of already known states.
- Symmetries in the observed spectrum?

## **Spin Observables in baryon production / decay**

- Reaction mechanism at different energy scales.
- The role of spin in the production of heavy quarks.
- CP violation



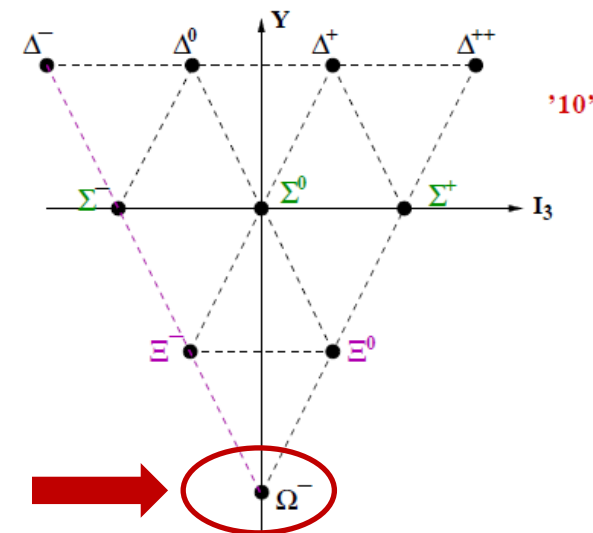
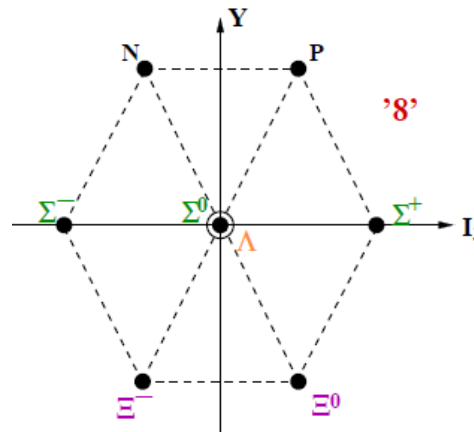
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# Part I: Baryon Spectroscopy



# Baryons and the quark model

- 1950's and 1960's: a multitude of new particles discovered → obvious they could not all be elementary
- 1961: Eight-fold way, organising mesons and spin  $\frac{1}{2}$  baryons into octets and spin  $\frac{3}{2}$  into a decuplet as a consequence of SU(3) flavour symmetry
- 1962: Discovery of the predicted  $\Omega^-$  demonstrates the success of the Eightfold way.
- 1964: Quark model (Gell-Mann and Zweig)





# Baryons and the quark model

- The simple (constituent) quark model\* was successful in classifying hadrons and describing some features of the hadron spectra.
- Unable to explain *e.g.*
  - Spin of the nucleon
  - Flavour asymmetry of the nucleon sea
  - Level ordering in light and strange baryon spectra\*\*

\*PR 125 (1962) 1067

\*\*PRD 58 (1998) 094030





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**The challenging task of baryon spectroscopy**

\*PR 125 (1962) 1067

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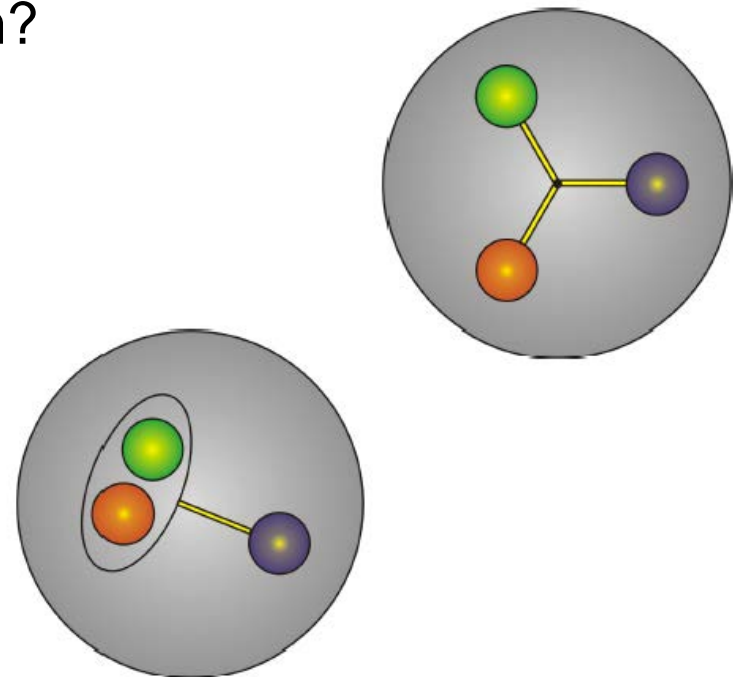


# Light baryon spectroscopy

A lot has been learned from the great progress in light baryon spectroscopy (pion beams, photoproduction).

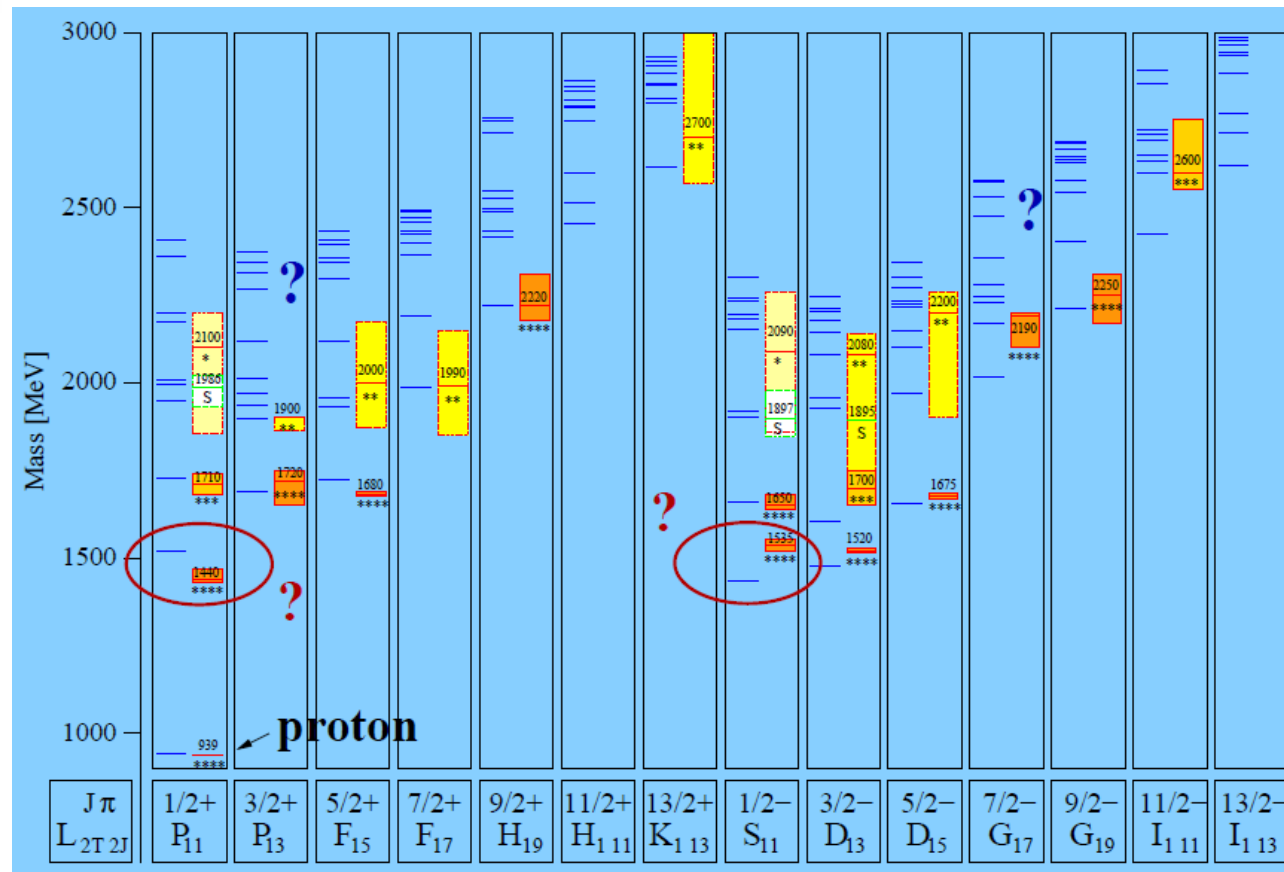
Open questions regarding the excited light baryon spectrum:\*

- Relevant degrees of freedom?
- Missing states
- High mass parity doublets
- Order of low mass positive and negative parity states  
(Roper and  $S_{11}(1535)$ )





# Light baryon spectroscopy



Missing states: # of observed states < # of predicted states

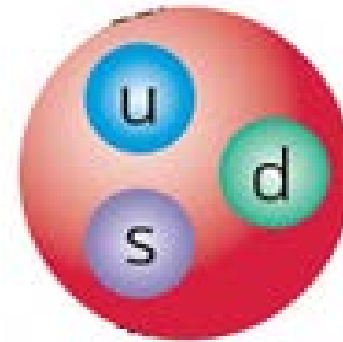
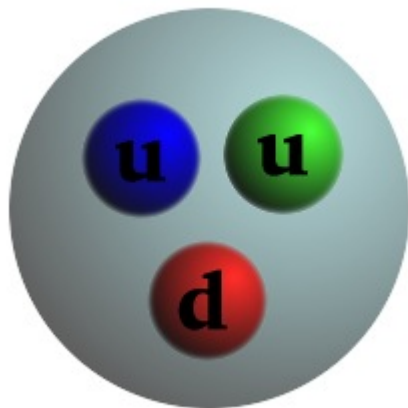
- Because there are no such states
- or because they do not couple to  $N\pi$  final states?



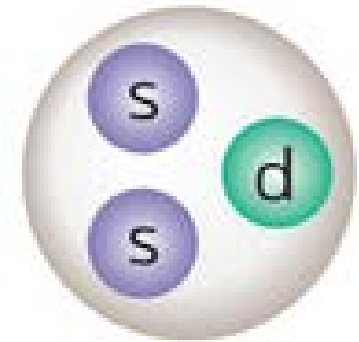
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# Strange (and charmed) hyperons

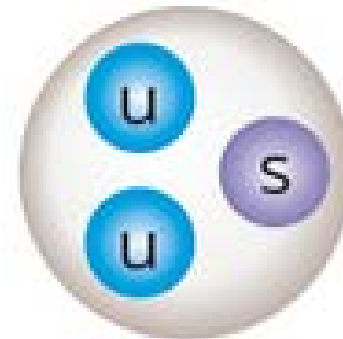
*What happens if  
we replace one of the  
light quarks in the proton  
with one - or many -  
heavier quark(s)?*



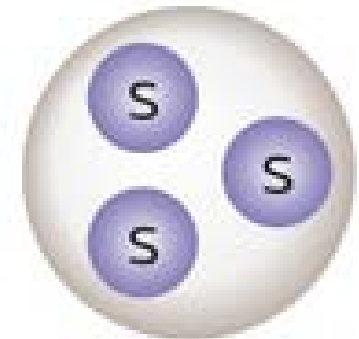
Lambda ( $\Lambda$ )



Xi ( $\Xi$ )



Sigma ( $\Sigma$ )



Omega ( $\Omega$ )



# Strange hyperons

Excited strange hyperon spectrum:

- $SU(6) \times O(3)$  classification (spin, flavour and  $L$ )
- Very scarce data bank on double and triple strangeness
- Octet  $\Xi$  partners of  $N^*$  ?
  - Only a few found
- Decuplet  $\Xi$  and  $\Omega$  partners of  $\Delta^*$  ?
  - Nothing found

$J^P$	$(D, L_N^P) S$	Octet members			Singlets
$1/2^+$	$(56, 0_0^+)$	$1/2 N(939)$	$\Lambda(1116)$	$\Sigma(1193)$	$\Xi(1318)$
$1/2^+$	$(56, 0_2^+)$	$1/2 N(1440)$	$\Lambda(1600)$	$\Sigma(1660)$	$\Xi(?)$
$1/2^-$	$(70, 1_1^-)$	$1/2 N(1535)$	$\Lambda(1670)$	$\Sigma(1620)$	$\Xi(?)$
$3/2^-$	$(70, 1_1^-)$	$1/2 N(1520)$	$\Lambda(1690)$	$\Sigma(1670)$	$\Xi(1820)$
$1/2^-$	$(70, 1_1^-)$	$3/2 N(1650)$	$\Lambda(1800)$	$\Sigma(1750)$	$\Xi(?)$
$3/2^-$	$(70, 1_1^-)$	$3/2 N(1700)$	$\Lambda(?)$	$\Sigma(?)$	$\Xi(?)$
$5/2^-$	$(70, 1_1^-)$	$3/2 N(1675)$	$\Lambda(1830)$	$\Sigma(1775)$	$\Xi(?)$
$1/2^+$	$(70, 0_2^+)$	$1/2 N(1710)$	$\Lambda(1810)$	$\Sigma(1880)$	$\Xi(?)$
$3/2^+$	$(56, 2_2^+)$	$1/2 N(1720)$	$\Lambda(1890)$	$\Sigma(?)$	$\Xi(?)$
$5/2^+$	$(56, 2_2^+)$	$1/2 N(1680)$	$\Lambda(1820)$	$\Sigma(1915)$	$\Xi(2030)$
$7/2^-$	$(70, 3_3^-)$	$1/2 N(2190)$	$\Lambda(?)$	$\Sigma(?)$	$\Xi(?)$
$9/2^-$	$(70, 3_3^-)$	$3/2 N(2250)$	$\Lambda(?)$	$\Sigma(?)$	$\Xi(?)$
$9/2^+$	$(56, 4_4^+)$	$1/2 N(2220)$	$\Lambda(2350)$	$\Sigma(?)$	$\Xi(?)$
Decuplet members					
$3/2^+$	$(56, 0_0^+)$	$3/2 \Delta(1232)$	$\Sigma(1385)$	$\Xi(1530)$	$\Omega(1672)$
$3/2^+$	$(56, 0_2^+)$	$3/2 \Delta(1600)$	$\Sigma(?)$	$\Xi(?)$	$\Omega(?)$
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$7/2^+$	$(56, 2_2^+)$	$3/2 \Delta(1950)$	$\Sigma(2030)$	$\Xi(?)$	$\Omega(?)$
$11/2^+$	$(56, 4_4^+)$	$3/2 \Delta(2420)$	$\Sigma(?)$	$\Xi(?)$	$\Omega(?)$





# Strange hyperons

- Are the states missing
  - because they are not there
  - or because previous experiments haven't been optimal for multistrange baryon search?
- PDG note on  $\Xi$  hyperons:
 

*“...nothing of significance on  $\Xi$  resonances has been added since our 1988 edition.”*
- Most previous experiments are performed with kaon beams
  - difficult to measure double and triple strange states

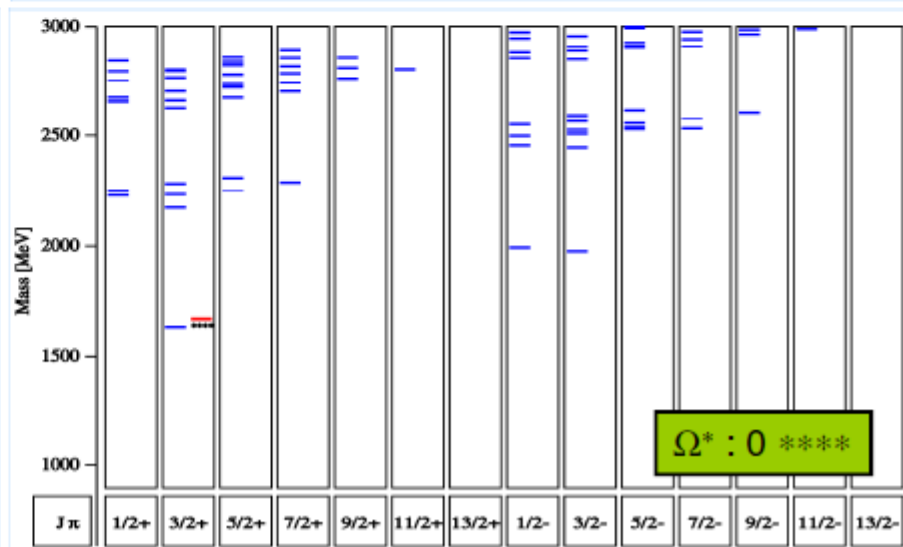
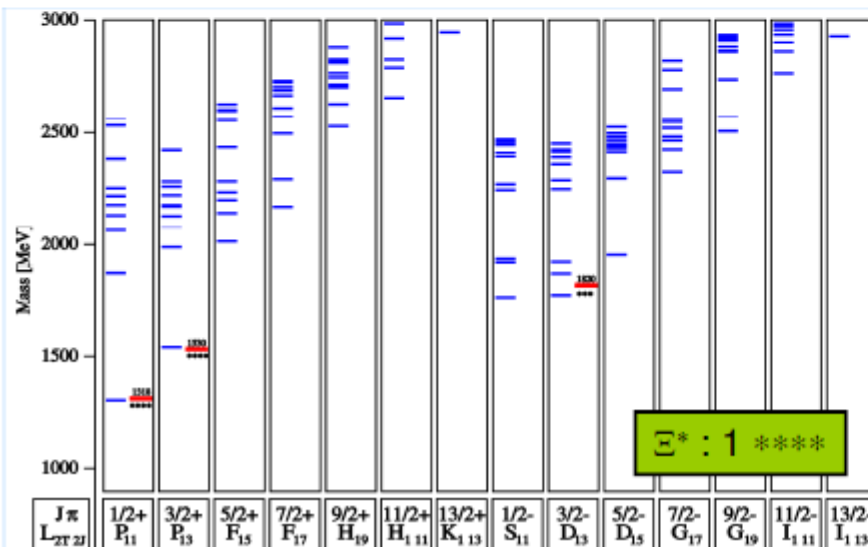
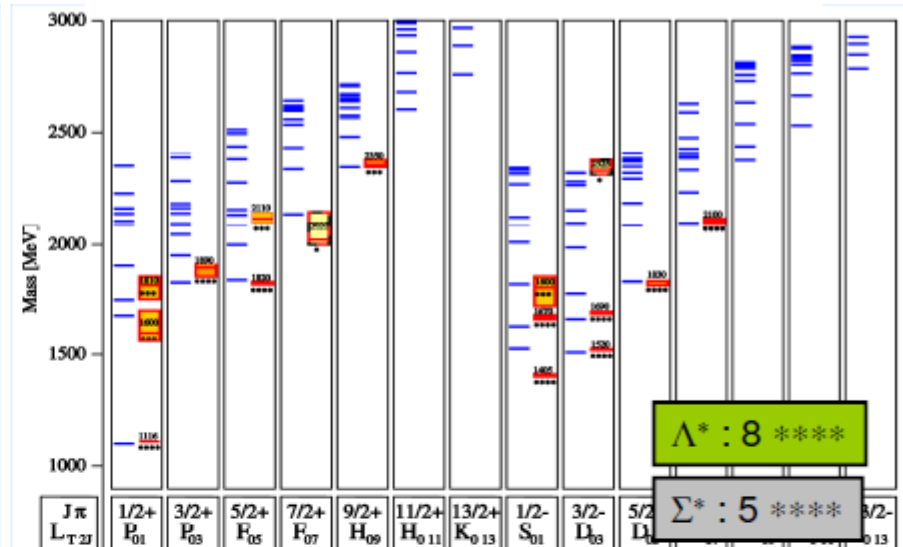
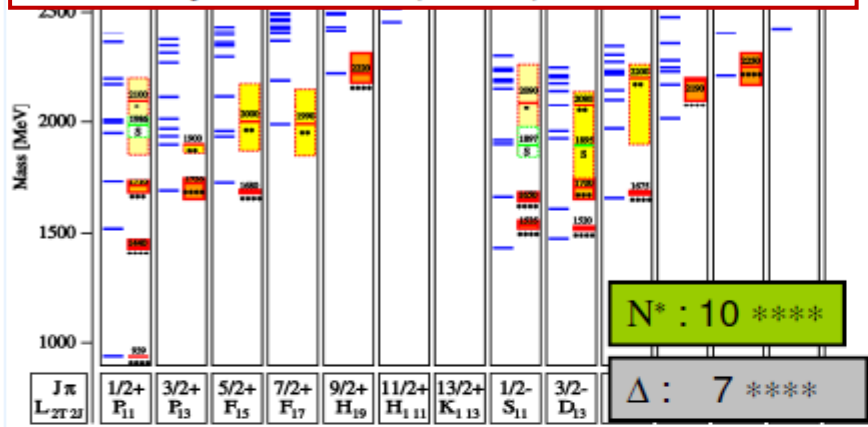
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# Strange hyperons

U. Löring, B.Ch. Metsch, H.R. Petry,  
Eur. Phys. J A 10 (2001) 309, 395, 447



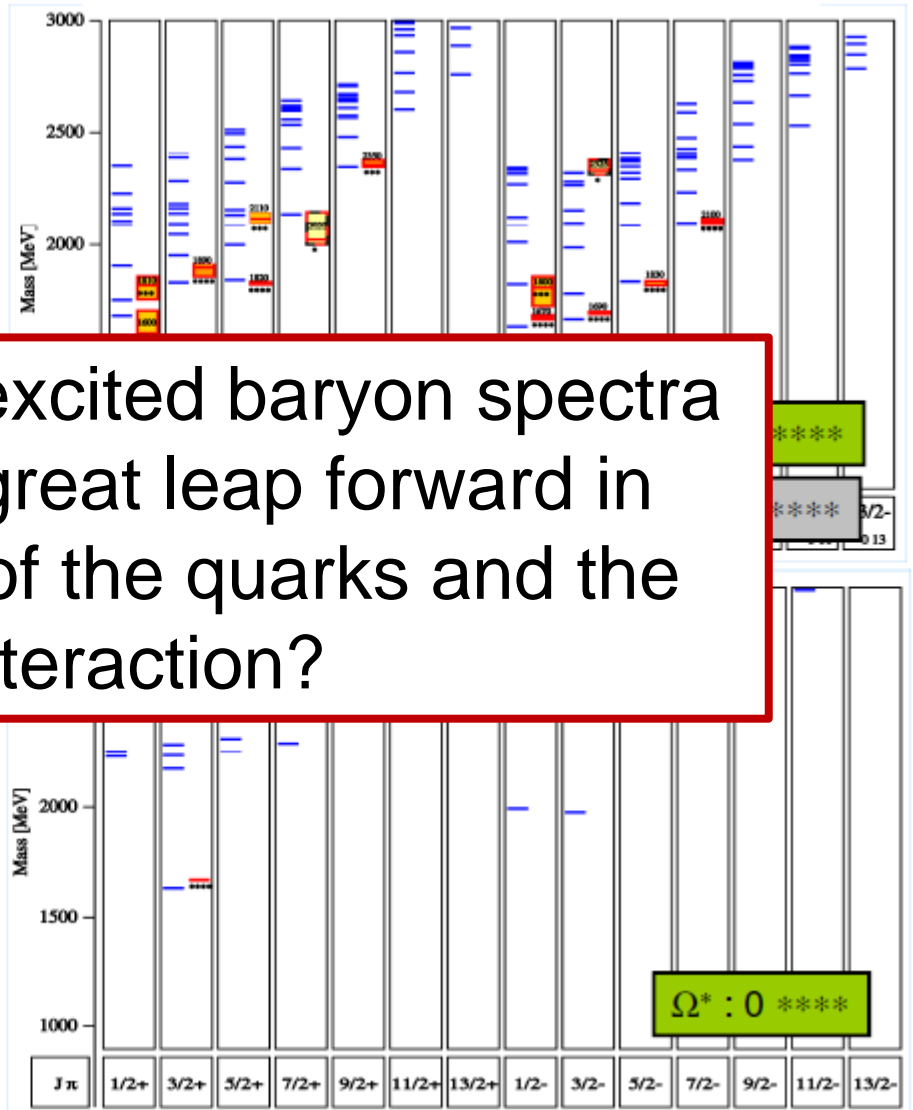
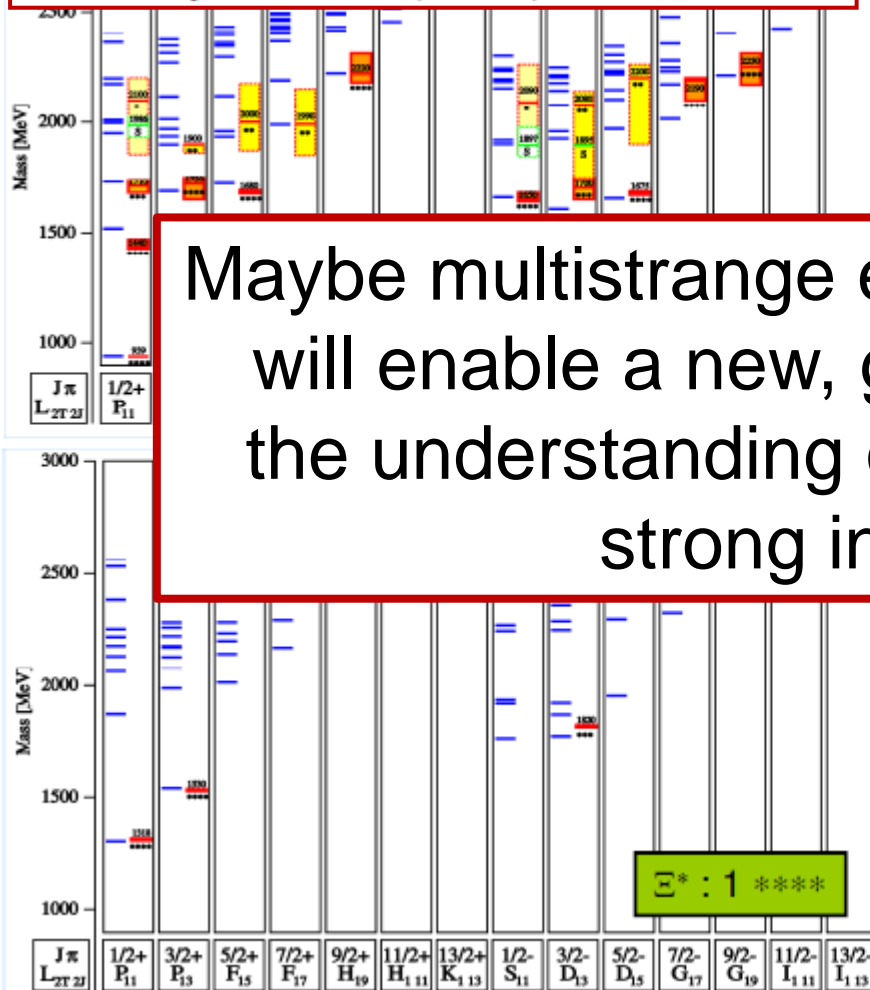


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Maybe multistrange excited baryon spectra  
will enable a new, great leap forward in  
the understanding of the quarks and the  
strong interaction?







# Prospects for PANDA

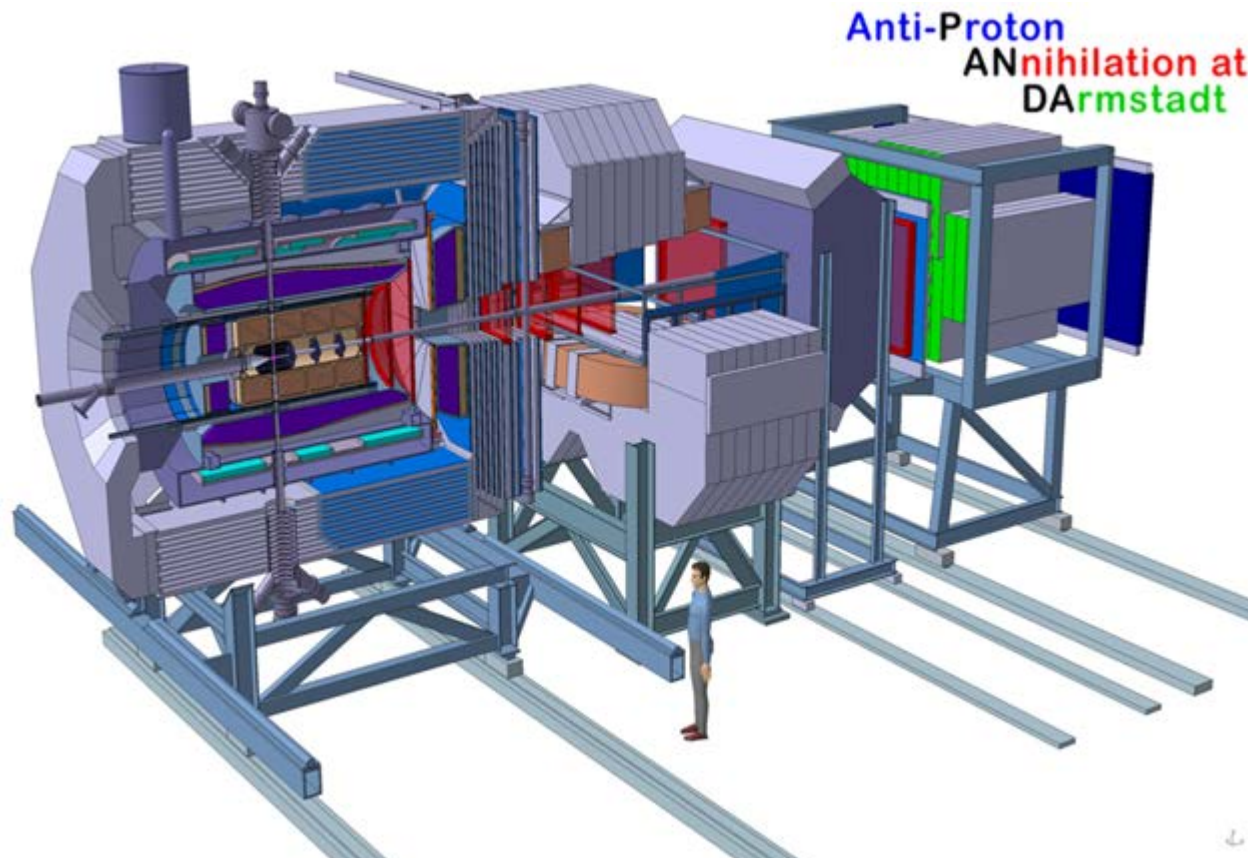
- A lot of previous and ongoing activity in light baryon spectroscopy (CLAS @ JLAB, CBELSA/TAPS)
  - Charmed baryons often bi-product at b-factories (BaBar, Belle, CLEO, LHCb)
- PANDA can fill the gap in the strange sector  
→ the full  $\Xi$  and  $\Omega$  spectra are accessible with PANDA!



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# Prospects for PANDA

- Antiprotons from HESR with momenta 1.5 -15 GeV/c.
- Unpolarised beam and target
- Near  $4\pi$  coverage
- Good momentum and vertex resolution.
- PID
- EM calorimetry





# Prospects for PANDA

- Large cross sections for  $\bar{p}p \rightarrow \bar{Y}Y^*$ 
  - $\bar{p}p \rightarrow \bar{\Xi}\Xi \approx \mu b$
  - $\bar{p}p \rightarrow \bar{\Omega}\Omega \approx 0.03 - 0.1 \mu b$
- No extra mesons in the final state needed for strangeness (or charm) conservation
- Symmetry in hyperon and antihyperon observables
- PANDA detector versatile (coverage, resolution, PID...)

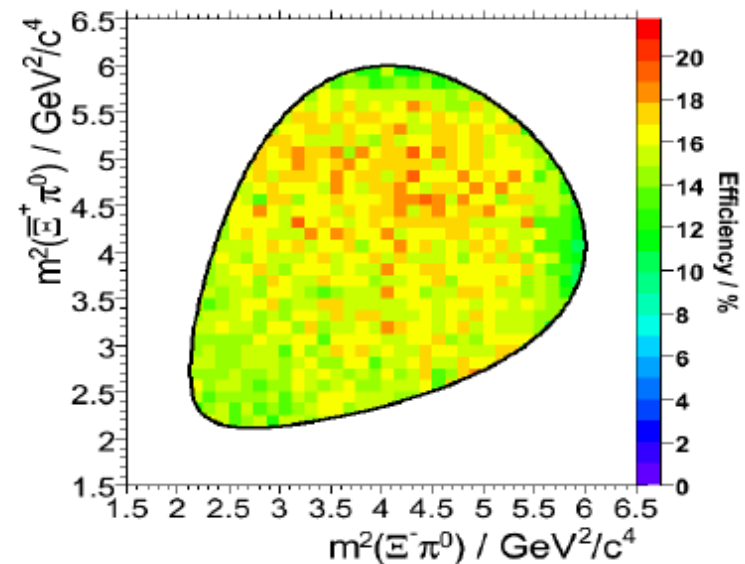
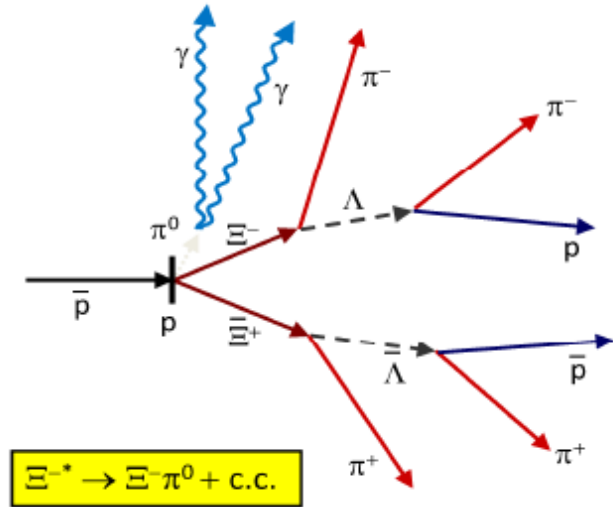
**PANDA is a unique experiment in baryon spectroscopy beyond  $N^*$  and  $\Delta$ !**



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# Feasibility study of $\bar{p}p \rightarrow \bar{\Xi}\Xi^*$

- $p_{beam} = 6.57 \text{ GeV}/c$
- $10^7$  MC events produced
- Consider the  $\Xi^{*-} \rightarrow \Xi^- \pi^0$  decay
- Background generated with DPM
- Simple MC framework taking efficiencies and detector resolution into account
- Results\*:
  - 10-20% efficiency
  - Smooth efficiency
  - $S/B > 19$



\* PANDA Physics Book (2009)



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# Baryon spectroscopy subtopics with PANDA

Study excited states of

- double-strange hyperons ( $\Xi^*$ )
- triple-strange hyperons ( $\Omega^*$ )
- charmed hyperons ( $\Lambda_c^*, \Sigma_c^*$ )
- hidden-charm nucleons ( $N_{c\bar{c}}$ )
- non-strange baryons ( $N^*$ )
- single-strange hyperons ( $\Lambda^*, \Sigma^*$ )



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# Part II: Spin Observables in Hyperon production





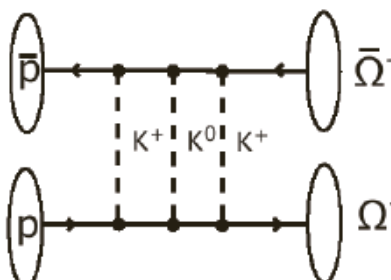
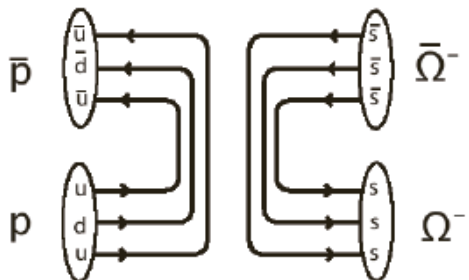
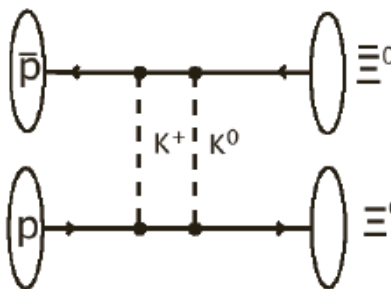
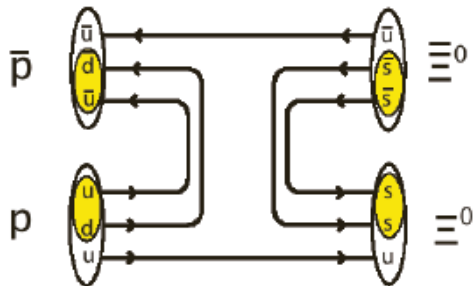
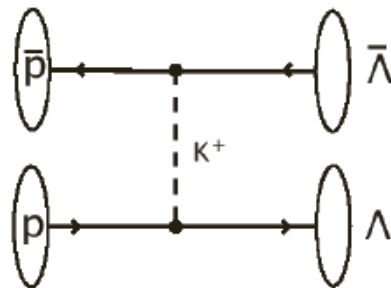
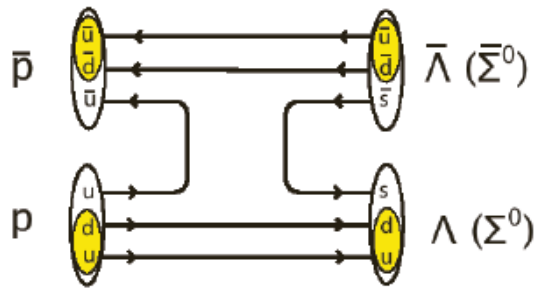
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Or: what can we learn from  
looking into detail how  
known hyperons  
are produced?



# Strange and charm production

Models based on the constituent quark-gluon picture\* and on the hadron picture\*\* or a combination of the two \*\*\*



Different models give different predictions of e.g.

- the polarisation of the outgoing hyperon
- the correlation of the spin of the hyperon-antihyperon

\*PLB 179 (1986) 15; PLB 165 (1985) 187;  
NPA 468 (1985) 669;

\*\* PRC 31(1985) 1857; PLB179 (1986) 15;  
PLB 214 (1988) 317;

\*\*\* PLB 696 (2011) 352.





# Spin observables in $\bar{p}p \rightarrow \bar{Y}Y$

Spin observables are powerful tools in testing models.

The spin density matrix  $\rho$  of a particle with arbitrary spin  $j$  is given by

$$\rho = \frac{1}{2j+1} \mathcal{I} + \sum_{L=1}^{2j} \rho^L \quad \text{with} \quad \rho^L = \frac{2j}{2j+1} \sum_{M=-L}^L Q_M^L r_M^L$$

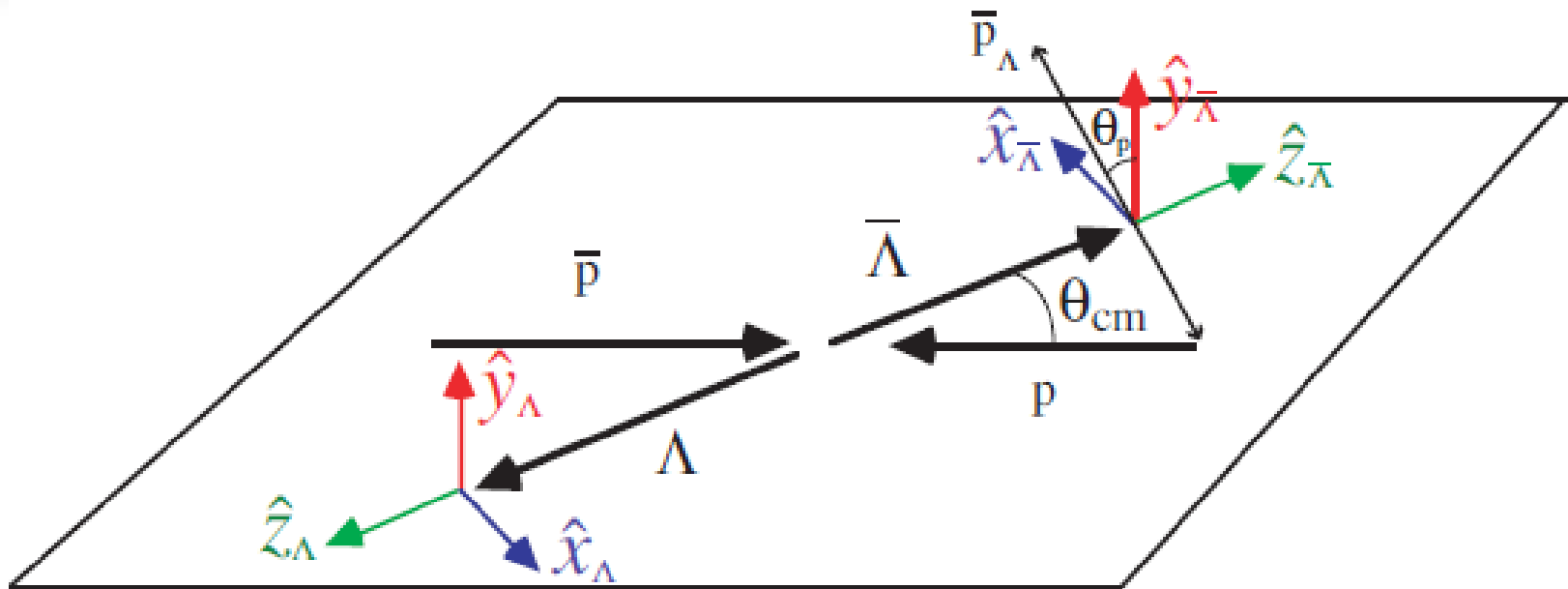
$\uparrow$   
Unpolarised

$\nwarrow$   
Polarised

where  $Q_M^L$  are hermitian matrices and  $r_M^L$  polarisation parameters.

- Spin  $\frac{1}{2}$  : **3** polarisation parameters:  $r_{-1}^1, r_0^1$  and  $r_1^1$ .
- Spin  $\frac{3}{2}$  : **15** polarisation parameters:  $r_{-1}^1, r_0^1, r_1^1, r_{-2}^2, r_{-1}^2, r_0^2, r_1^2, r_2^2, r_{-3}^3, r_{-2}^3, r_{-1}^3, r_0^3, r_1^3, r_2^3$  and  $r_3^3$ .
- Degree of polarisation given by:  $d(\rho) = \sqrt{\sum_{L=1}^{2j} \sum_{M=-L}^L (r_M^L)^2}$

# Spin observables for spin $\frac{1}{2}$ hyperons



- The  $Q_M^L$  from  $\rho^L = \frac{2j}{2j+1} \sum_{M=-L}^L Q_M^L r_M^L$  are the Pauli matrices.
- Polarisation parameters  $r_0^1$ ,  $r_{-1}^1$  and  $r_1^1$  denoted  $P_x$ ,  $P_y$  and  $P_z$ .
- Symmetry from parity conservation (strong production) requires  $P_x = P_z = 0$   
 → **polarisation normal of the production plane!**



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# Spin observables for spin $\frac{1}{2}$ hyperons

Hyperons decay weakly:

→ decay matrix has one **parity conserving** part and one **parity violating** part.

Parity violating:

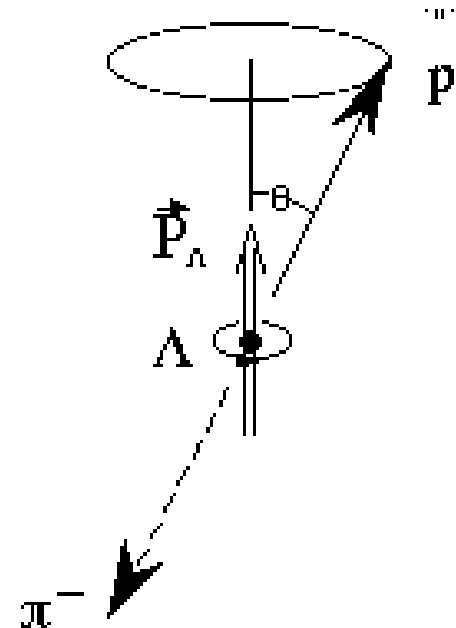
→ daughter particles are according to the polarisation of the mother hyperon.

Angular distribution is given by

$$I(\cos\theta_p) = N(1 + \alpha P_Y \cos\theta_p)$$

$\alpha$ : decay parameter related to the decay matrix.

→ The polarisation is accessible by the angular distribution of the decay products!

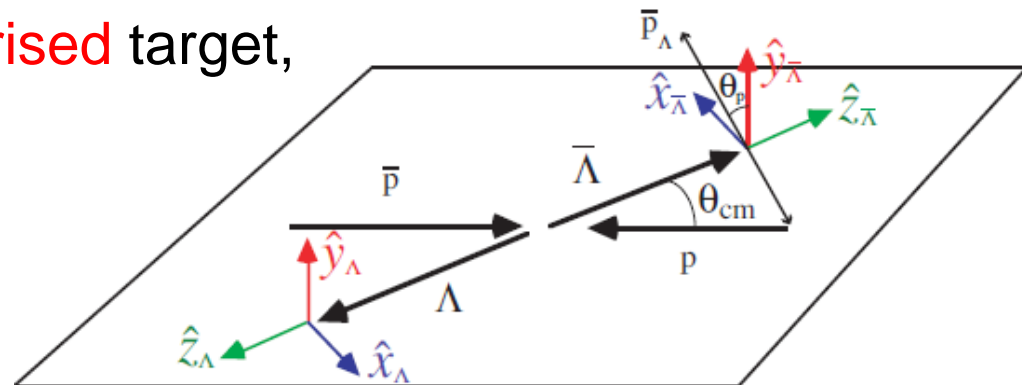


# Spin observables for spin $\frac{1}{2}$ hyperons

Polarised Particle	None	Beam	Target	Both
None	$I_{0000}$	$A_{i000}$	$A_{0j00}$	$A_{ij00}$
Scattered	$P_{00\mu 0}$	$D_{i0\mu 0}$	$K_{0j\mu 0}$	$M_{ij\mu 0}$
Recoil	$P_{000\nu}$	$K_{i00\nu}$	$D_{0j0\nu}$	$N_{ij0\nu}$
Both	$C_{00\mu\nu}$	$C_{i0\mu\nu}$	$C_{0j\mu\nu}$	$C_{ij\mu\nu}$

In the  $\bar{p}p \rightarrow \bar{Y}Y$  reaction there are 256 spin variables.

**Unpolarised** beam and **unpolarised** target,  
the polarisation  $P_{00y0}$  and  $P_{000y}$   
and the spin correlations  
 $C_{00\nu\mu}$  ( $\nu, \mu = x, y, z$ )  
are accessible.



# Spin observables for spin $\frac{3}{2}$ hyperons

The  $p\bar{p} \rightarrow \Omega\bar{\Omega}$  reaction:

**15** polarisation parameters, **7** are accessible in  $\Omega \rightarrow \Lambda K$  with an unpolarised beam and target.

**3** polarisation parameters  $r_2^2$ ,  $r_1^2$ ,  $r_0^2$  can be retrieved from the angular distribution of the  $\Lambda^*$ , assuming  $\alpha_\Omega = 0$  consistent with experiment.\*\*

$$r_0^2 = \frac{15}{2\sqrt{3}} \left( \frac{1}{3} - \langle \cos^2 \theta_\Lambda \rangle \right)$$

$$r_2^2 = \frac{8}{3} \left( 1 - \langle \cos^2 \theta_\Lambda \rangle - 2 \langle \sin^2 \theta_\Lambda \sin^2 \phi_\Lambda \rangle \right)$$

$$r_1^2 = 5 \langle \cos \theta_\Lambda \sin \theta_\Lambda \cos \phi_\Lambda \rangle$$

\*\*Erik Thomé, *Multistrange and Charmed Antihyperon-Hyperon Physics for PANDA*  
Ph. D. Thesis, Uppsala University (2012)

\*\* PDG, J. Phys. G 33 (2006) 1.



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# Spin observables for spin $\frac{3}{2}$ hyperons

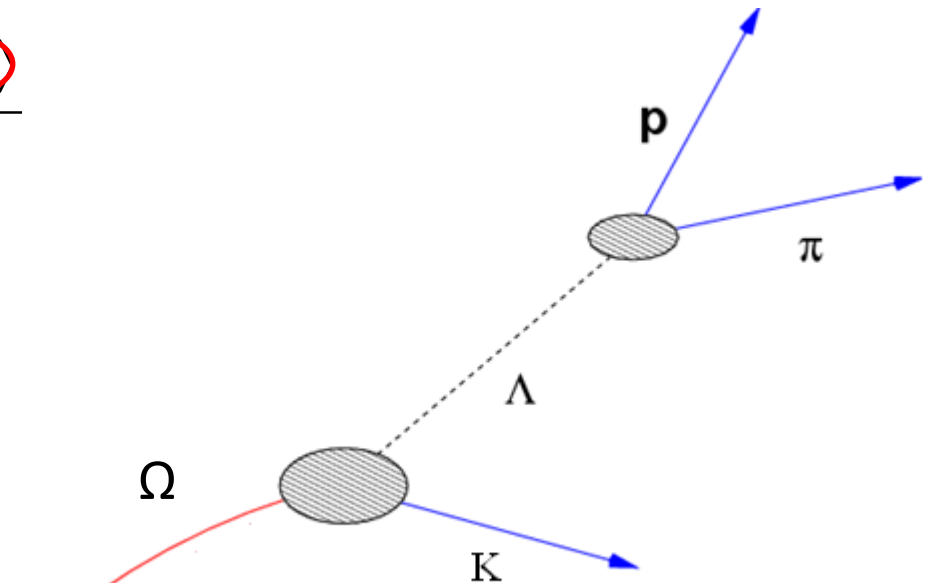
Four polarisation parameters can be determined from the joint angular distributions of the  $\Lambda$  and the proton \*:

$$r_{-1}^1 = - \frac{20\sqrt{10} \langle (3\cos\theta_\Lambda - 1) \sin\phi_p \rangle}{3\pi\alpha_\Lambda\gamma_\Omega}$$

$$r_{-1}^3 = \frac{2\sqrt{5} \langle (15\cos\theta_\Lambda - 1) \sin\phi_p \rangle}{\sqrt{3}\pi\alpha_\Lambda\gamma_\Omega}$$

$$r_{-2}^3 = - \frac{1024 \langle \sin\phi_\Lambda \cos\phi_p \rangle}{3\pi^2\alpha_\Lambda\gamma_\Omega}$$

$$r_{-3}^3 = - \frac{1}{5\sqrt{6}} \left( \frac{640}{\pi\alpha_\Lambda\gamma_\Omega} \langle \sin\phi_\Lambda \cos\phi_\Lambda \sin\phi_p \rangle + 4\sqrt{15}r_{-1}^3 + 3\sqrt{10}r_{-1}^1 \right)$$



$\alpha, \beta, \gamma$  decay parameters.  
Assume:  $\alpha_\Omega = 0, \beta_\Omega \approx 0$

\*Erik Thomé, Ph. D. Thesis and later work



# Spin observables in $\bar{p}p \rightarrow \bar{Y}Y$

- Spin  $\frac{1}{2}$  hyperons ( $\Lambda$ ,  $\Xi$ ,  $\Lambda_c$ ):
  - Polarisation.
  - Spin correlations and singlet fraction:
$$SF = \frac{1}{4}(1 + C_{xx} - C_{yy} + C_{zz})$$
- Spin  $\frac{3}{2}$  hyperons into spin  $\frac{1}{2}$  hyperons ( $\Omega \rightarrow \Lambda K$ ):
  - 7 polarisation parameters + degree of polarisation.

$$d(\rho) = \sqrt{\sum_{L=1}^{2j} \sum_{M=-L}^L (r_M^L)^2}$$



# CP violation in hyperon systems

- CP violation of baryon system has never been observed.
- The  $\bar{p}p \rightarrow \bar{Y}Y$  process suitable for CP measurements (clean, no mixing)
- According to experiment,  $\alpha = \bar{\alpha}$  for  $\Lambda$ .
- CP violation parameters:

$$A = \frac{\Gamma\alpha + \bar{\Gamma}\bar{\alpha}}{\Gamma\alpha - \bar{\Gamma}\bar{\alpha}} \approx \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}}$$

Consistent with 0 for  $\Lambda$  and  $\Xi$ , but to confirm or rule out or confirm  $\chi$ PT, Supersymmetry, more precise measurements are needed.

$$B = \frac{\Gamma\beta + \bar{\Gamma}\bar{\beta}}{\Gamma\beta - \bar{\Gamma}\bar{\beta}} \approx \frac{\beta + \bar{\beta}}{\beta - \bar{\beta}}$$

Accessible for  $\Xi$  since the polarisation of the decay products can be measured.

$$B' = \frac{\Gamma\beta + \bar{\Gamma}\bar{\beta}}{\Gamma\alpha - \bar{\Gamma}\bar{\alpha}} \approx \frac{\beta + \bar{\beta}}{\alpha - \bar{\alpha}}$$

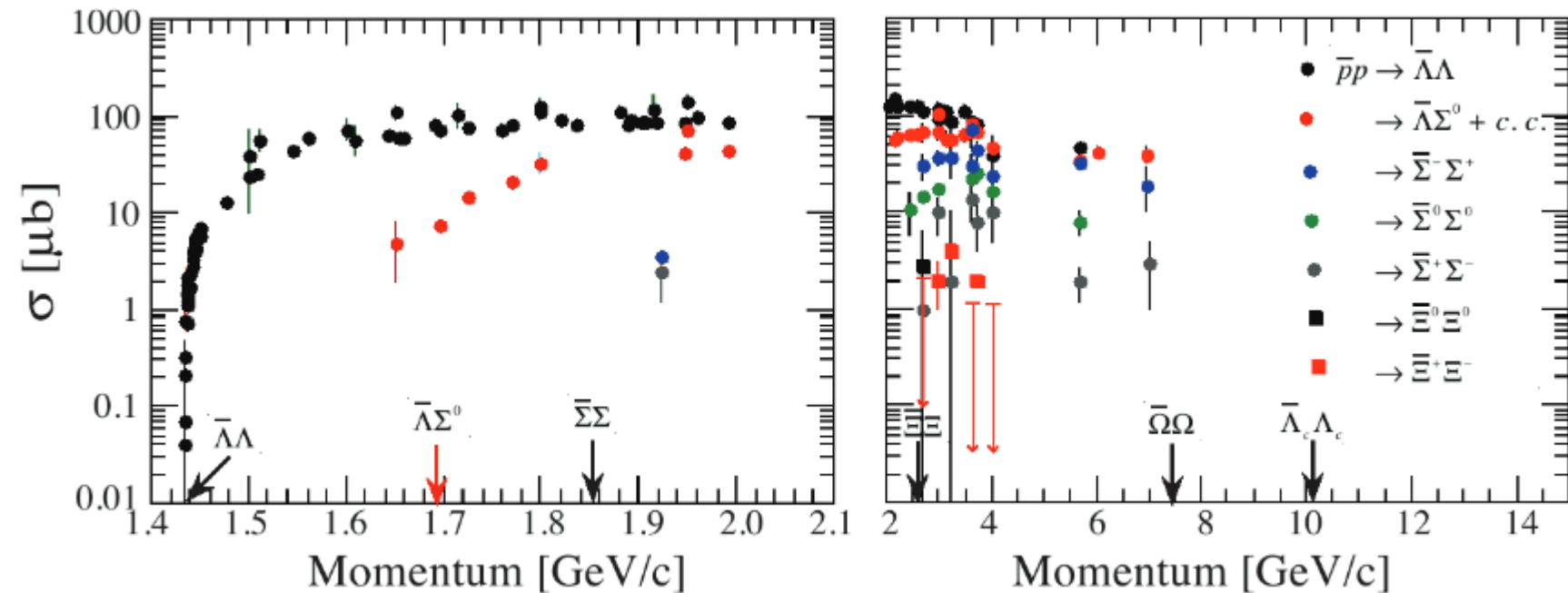
No previous measurement.





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# Previous measurements of $\bar{p}p \rightarrow \bar{Y}Y$

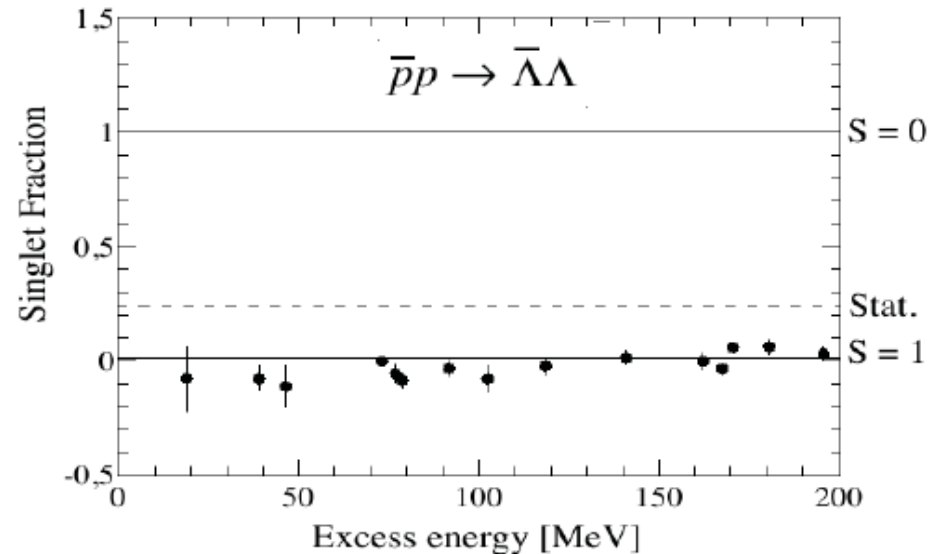
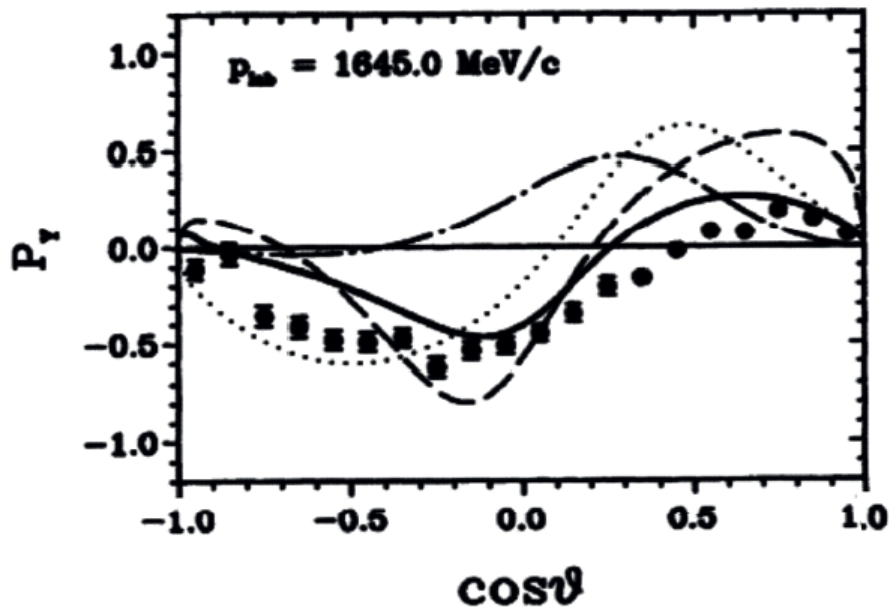


- A lot of data on  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  near threshold, mainly from PS185 at LEAR\*.
- Very scarce data bank above 4 GeV.
- Only a few bubble chamber events on  $\bar{p}p \rightarrow \bar{\Xi}\Xi$
- No data on  $\bar{p}p \rightarrow \bar{\Omega}\Omega$  nor  $\bar{p}p \rightarrow \bar{\Lambda}_c\Lambda_c$

\* See e.g. T. Johansson, AIP Conf. Proc. Of LEAP 2003, p. 95.



# Previous measurements of $\bar{p}p \rightarrow \bar{Y}Y$



- $\bar{\Lambda}\Lambda$  almost always produced in a spin triplet state\*:

$$SF = \frac{1}{4}(1 + C_{xx} - C_{yy} + C_{zz})$$

- Neither the quark-gluon picture (dotted) nor hadron exchange (solid and dashed) describe polarisation data perfectly. \*\*

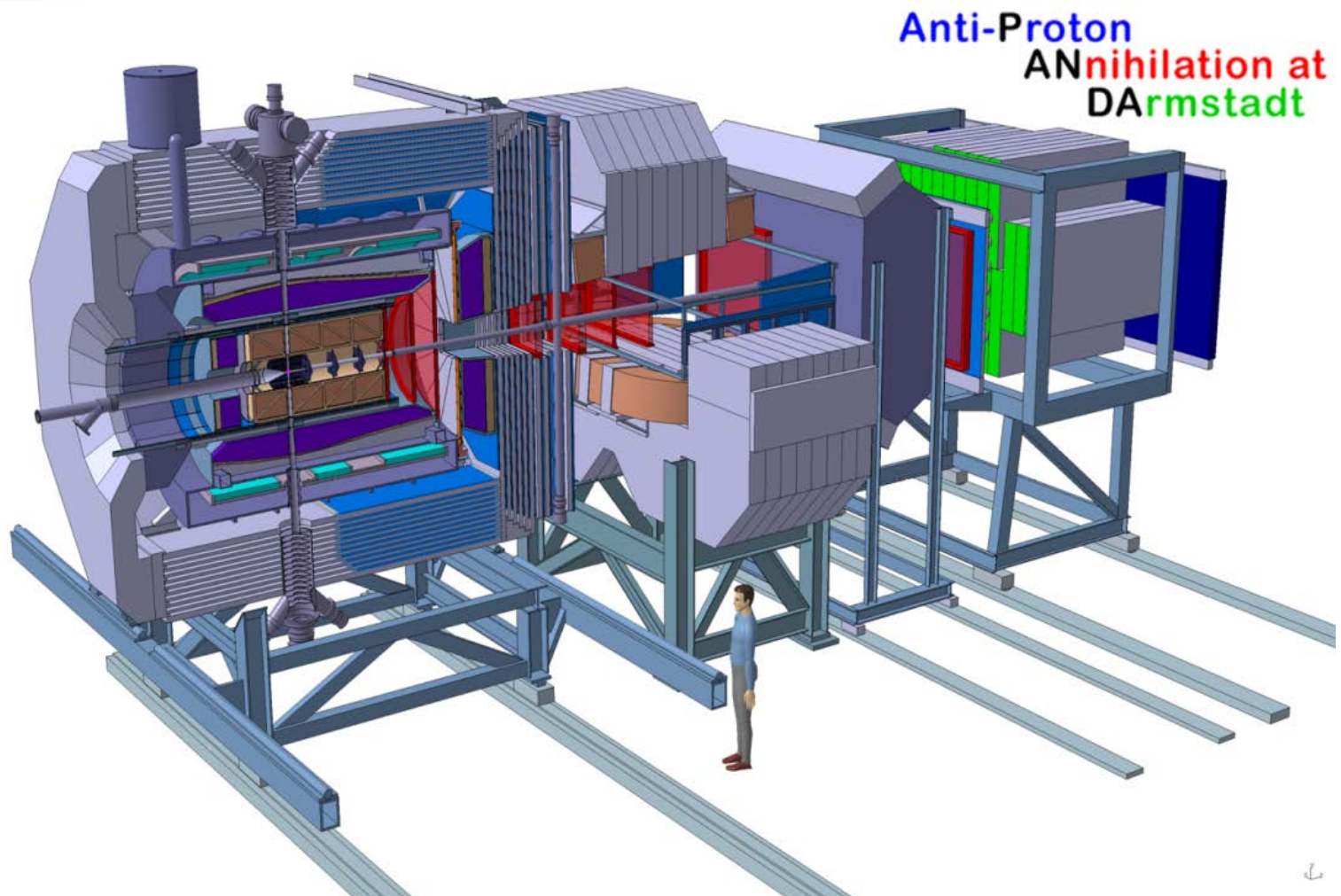
\*PRC 54 (1996) 1877

\*\* Phys. Rep. 368 (2002) 119.



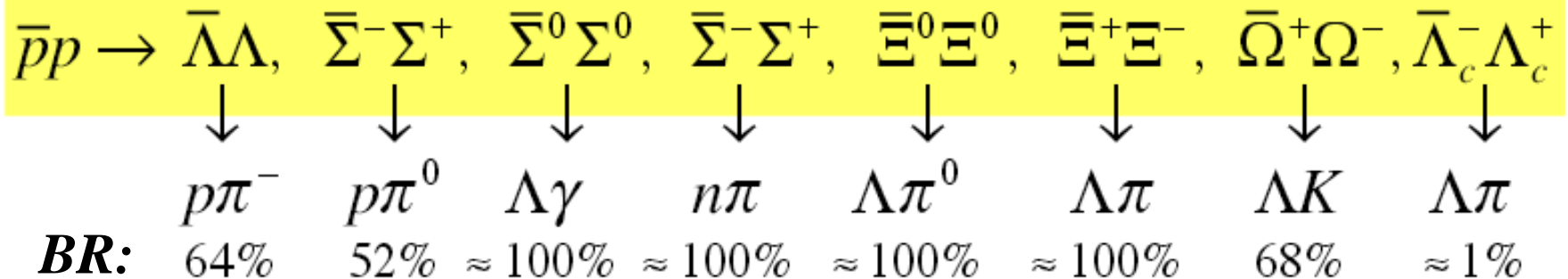
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# Prospects for PANDA





# Prospects for PANDA



- Simulation studies using a simplified MC framework (smearing and acceptance included)
- Quoted rates are valid for high luminosity mode of the HESR ( $2 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ ).
- Cross sections of  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  and  $\bar{p}p \rightarrow \bar{\Lambda}\Sigma^0$  known near threshold, the  $\bar{p}p \rightarrow \bar{\Xi}^+\Xi^-$  measured with large uncertainty.
- Only theoretical predictions of  $\bar{p}p \rightarrow \bar{\Omega}^+\Omega^-$  and  $\bar{p}p \rightarrow \bar{\Lambda}_c^-\Lambda_c^+$



# Prospects for PANDA

Momentum (GeV/c)	Reaction	$\sigma$ ( $\mu\text{b}$ )	Efficiency (%)	Rate (high lumi. mode)
1.64	$\bar{p}p \rightarrow \bar{\Lambda}\Lambda$	64	10	$580 \text{ s}^{-1}$
4	$\bar{p}p \rightarrow \bar{\Lambda}\Sigma^0$	$\sim 40$	30	$600 \text{ s}^{-1}$
4	$\bar{p}p \rightarrow \bar{\Xi}^+\Xi^-$	$\sim 2$	20	$30 \text{ s}^{-1}$
12	$\bar{p}p \rightarrow \bar{\Omega}^+\Omega^-$	$\sim 0.002$	30	$\sim 80 \text{ h}^{-1}$
12	$\bar{p}p \rightarrow \bar{\Lambda}_c^-\Lambda_c^+$	$\sim 0.1$	35	$\sim 25 \text{ day}^{-1}$

- High event rates for  $\Lambda$  and  $\Sigma$  \*.
- Low background for  $\Lambda$  and  $\Sigma$  \*.
- Even with conservative cross section estimates,  $\Omega$  and  $\Lambda_c$  channels are feasible. \*\*
- New efficiencies obtained with a more sophisticated MC framework are underway.

\*Sophie Grape, Ph. D. Thesis, Uppsala University 2009

\*\* Erik Thomé, Ph. D. Thesis, Uppsala University 2012

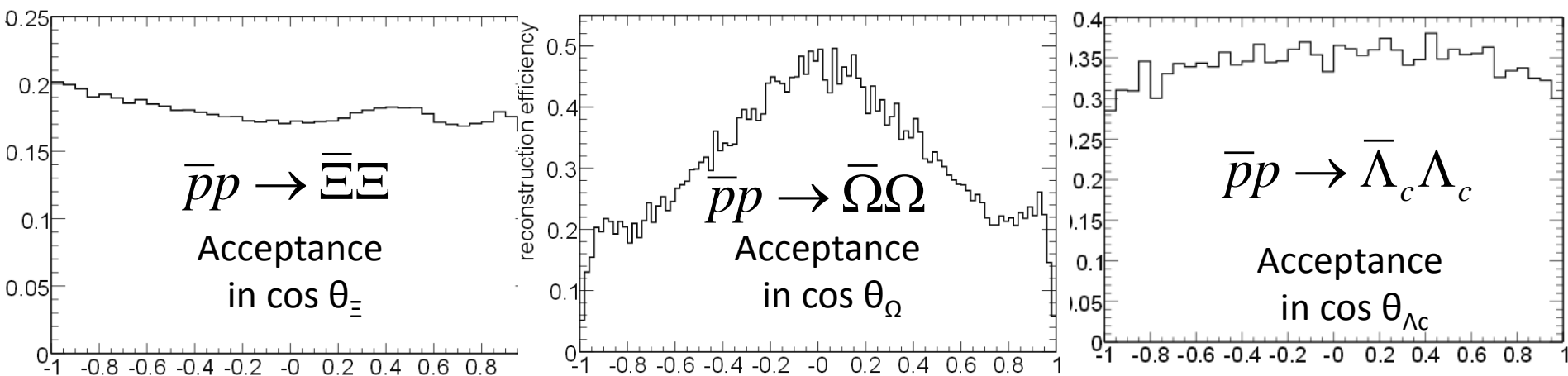




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# Prospects for PANDA

Good angular acceptance also for heavy hyperons  $\rightarrow$  important for polarisation studies!



Results by Erik Thomé, Ph. D. Thesis, Uppsala University (2012).



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# Prospects for PANDA at FAIR

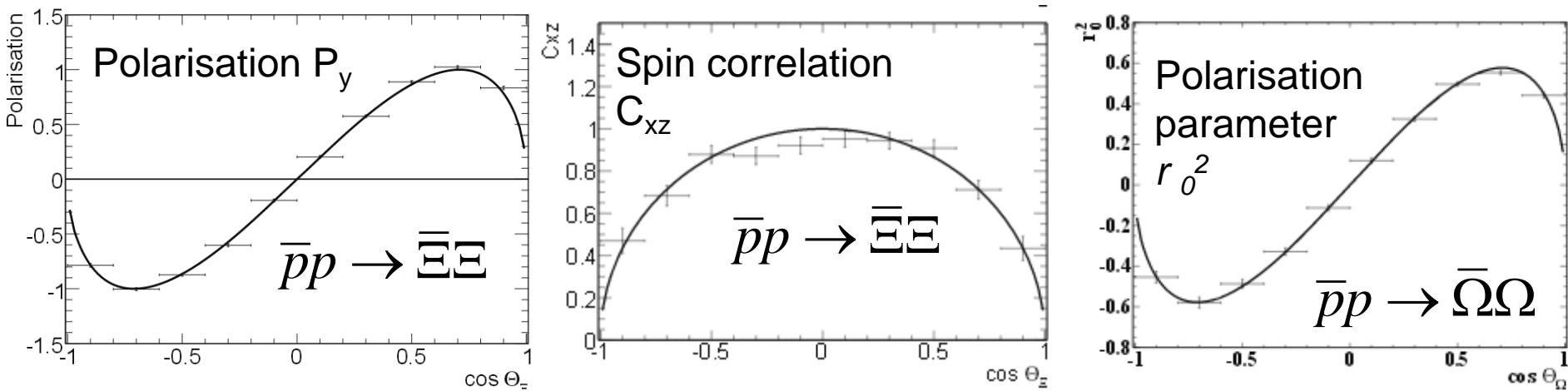
- Parametrisation of spin variables using weights:

$$P_{\Xi,y} = \sin 2\theta_{\Xi}$$

$$C_{\Xi,xz} = \sin \theta_{\Xi}$$

$$r_0^2 = \sin 2\theta_{\Omega} / \sqrt{3}$$

- Simplifies MC framework including acceptance and detector resolution.



- The polarisation and spin correlations for  $\Xi$  and polarisation parameters of the  $\Omega$  can be well reconstructed with PANDA.



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# Summary and Outlook

- Strange hyperons probe the Strong Interaction in the confinement domain.
- Several open questions in baryon spectroscopy show that there is much more to learn on how quarks interact inside baryons.
- What happens if light quarks are replaced with heavier? Very little is known about the excited strange hyperon spectra.
- PANDA can fill a gap in the strange sector
- Production of strange and charmed hyperons probe QCD at two different energy scales.
- Polarisation parameters of  $p\bar{p} \rightarrow \Omega\bar{\Omega}$  have been derived.
- Simulation studies show excellent prospects for antihyperon-hyperon channels with PANDA.

Thanks to: Albrecht Gillitzer,  
Stefan Leupold, Sophie Grape,  
Tord Johansson and Erik Thomé







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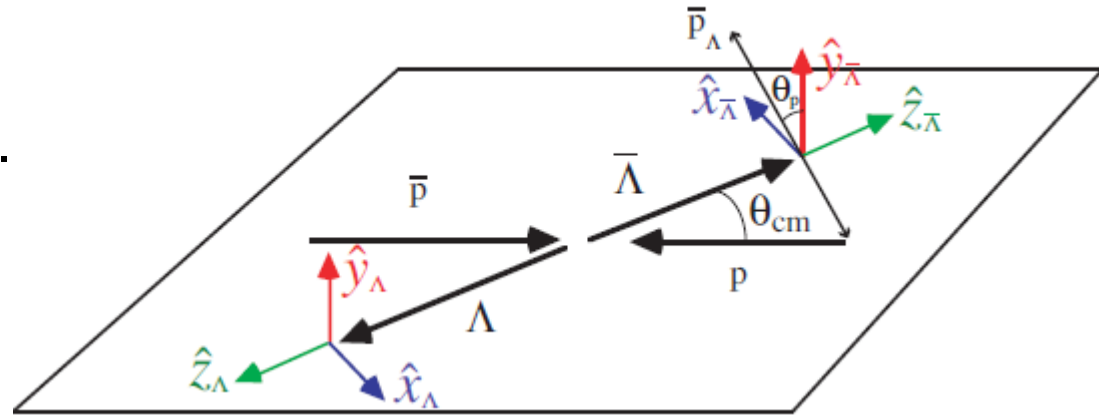
# Backup



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# Spin observables for spin $\frac{1}{2}$ hyperons

- The  $Q_M^L$  are the Pauli matrices.
- Polarisation parameters  $r_0^1$ ,  $r_{-1}^1$  and  $r_1^1$  are  $P_x$ ,  $P_y$  and  $P_z$ .



The spin density matrix of one spin  $\frac{1}{2}$  particle is given by:

$$\rho(1/2) = \frac{1}{2}(\mathcal{I} + \bar{\mathbf{P}} \cdot \bar{\boldsymbol{\sigma}}) = \frac{1}{2} \begin{bmatrix} 1 + P_z & P_x + iP_y \\ P_x - iP_y & 1 - P_z \end{bmatrix}$$

Symmetry from parity conservation (strong production) requires  $P_x = P_z = 0 \rightarrow$

$$\rho(1/2) = \frac{1}{2} \begin{bmatrix} 1 & iP_y \\ -iP_y & 1 \end{bmatrix}$$

**Polarisation normal  
to the production  
plane!**



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# Spin observables for spin $\frac{1}{2}$ hyperons

Parity violating decay  $\rightarrow$  direction of the decay products depends on the polarisation of the mother hyperon.

Angular distribution of the final state is given by  $I(\theta, \varphi) = \text{Tr}(T\rho T^*)$

Decay matrix  $T$  consists of

$T_s$  (s-wave, parity conserving) and  $T_p$  (p-wave, parity violating)

$$\alpha = 2\text{Re}(T_s^* T_p)$$

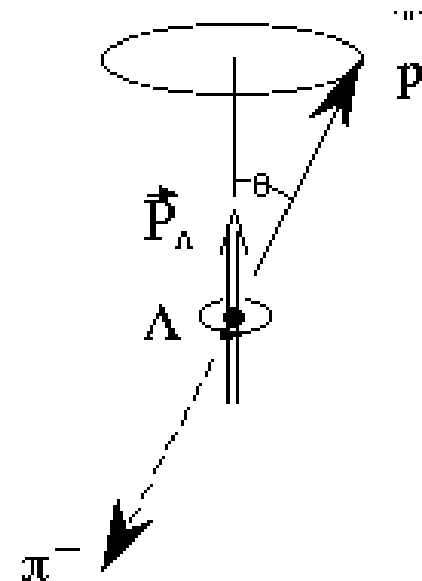
Define:  $\beta = 2\text{Im}(T_s^* T_p)$

$$\gamma = |T_s|^2 - |T_p|^2$$

Then  $\alpha^2 + \beta^2 + \gamma^2 = |T_s|^2 + |T_p|^2 = 1$

and the decay angular distribution becomes

$$I(\cos\theta_p) = N(1 + \alpha P_Y \cos\theta_p)$$





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# Spin observables for spin $\frac{1}{2}$ hyperons

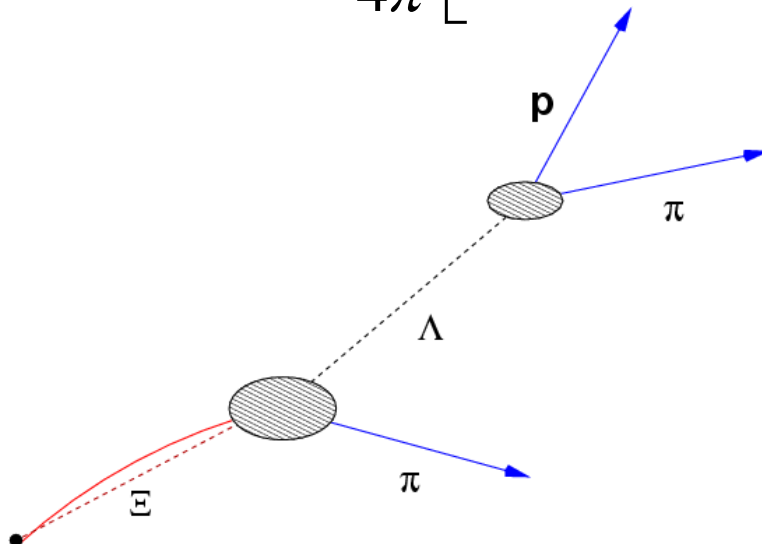
If the decay product of the hyperon is a hyperon, e.g.  $\Xi \rightarrow \Lambda K$ , then also  $\beta$  and  $\gamma$  can be obtained from the decay protons of the  $\Lambda$ .

Redefine reference system such that:

- Spin of  $\Xi$  along  $\hat{z}$
- $p_\Lambda$  in xz-plane ( $p_y = 0$ )

Then the proton angular distribution becomes:

$$I(\theta_p, \phi_p) = \frac{1}{4\pi} \left[ 1 + \alpha_\Xi \alpha_\Lambda \cos \theta_p + \frac{\pi}{4} \alpha_\Lambda P \sin \theta_p (\beta_\Xi \sin \phi_p - \gamma_\Xi \cos \phi_p) \right]$$





# Spin observables for spin $\frac{1}{2}$ hyperons

## Method of Moments

The expectation value or the moment of a function  $g(x)$  can be written

$$\langle g(x) \rangle = \int_{\Omega} g(x) f(x | \theta) dx$$

where  $f(x|\theta)$  is a probability density function.

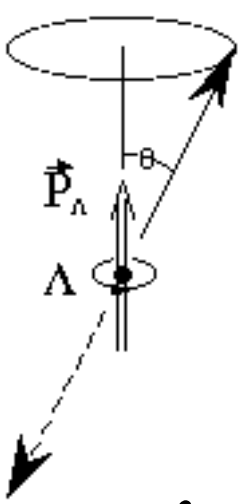
Example:  $\Lambda$  hyperon with polarisation  $P_n$  decaying into  $p \pi^-$ . Then

$$f(\theta_p | P_n) = \frac{dN}{d \cos \theta_p} \propto 1 + \alpha_{\Lambda} P_n \cos \theta_p$$

and thus

$$\langle \cos \theta_p \rangle = \int \frac{dN}{d \cos \theta_p} \cos \theta_p d \cos \theta_p = \int (1 + \alpha_{\Lambda} P_n \cos \theta_p) \cos \theta_p d \cos \theta_p = \frac{\alpha_{\Lambda} P_n}{3}$$

which means that the polarisation can be expressed as  $P_n = \frac{3}{\alpha_{\Lambda}} \langle \cos \theta_p \rangle$





# CP violation in hyperon systems

- CP violation of baryon system has never been observed.
- The  $\bar{p}p \rightarrow \bar{Y}Y$  process suitable for CP measurements (clean, no mixing)
- According to experiment,  $\alpha = \bar{\alpha}$  for  $\Lambda$ .
- CP violation parameters:

$$A = \frac{\Gamma\alpha + \bar{\Gamma}\bar{\alpha}}{\Gamma\alpha - \bar{\Gamma}\bar{\alpha}} \approx \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}}$$

Consistent with 0 for  $\Lambda$  and  $\Xi$ , but to confirm or rule out or confirm  $\chi$ PT, Supersymmetry, more precise measurements are needed.

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Accessible for  $\Xi$  since the polarisation of the decay products can be measured.

$$B' = \frac{\Gamma\beta + \bar{\Gamma}\bar{\beta}}{\Gamma\alpha - \bar{\Gamma}\bar{\alpha}} \approx \frac{\beta + \bar{\beta}}{\alpha - \bar{\alpha}}$$

No previous measurement.



# Spin observables for spin $\frac{3}{2}$ hyperons

This case much more complicated.

Erik Thomé has derived the observables in his Ph. D. thesis.\*

The spin density matrix is given by

$$\rho(3/2) = \frac{1}{4} \begin{bmatrix} 1 + \sqrt{3}r_0^2 & i\frac{3}{\sqrt{5}}r_{-1}^1 - \sqrt{3}r_1^2 & \sqrt{3}r_2^2 - i\sqrt{3}r_{-2}^3 & -i\sqrt{6}r_{-3}^3 \\ -i\frac{3}{\sqrt{5}}r_{-1}^1 - \sqrt{3}r_1^2 & 1 - \sqrt{3}r_0^2 & i2\sqrt{\frac{3}{5}}r_{-1}^1 + i3\sqrt{\frac{2}{5}}r_{-1}^3 & \sqrt{3}r_2^2 + i\sqrt{3}r_{-2}^3 \\ \sqrt{3}r_2^2 + i\sqrt{3}r_{-2}^3 & -i2\sqrt{\frac{3}{5}}r_{-1}^1 - i3\sqrt{\frac{2}{5}}r_{-1}^3 & 1 - \sqrt{3}r_0^2 & i\frac{3}{\sqrt{5}}r_{-1}^1 + \sqrt{3}r_1^2 \\ i\sqrt{6}r_{-3}^3 & \sqrt{3}r_2^2 - i\sqrt{3}r_{-2}^3 & -i\frac{3}{\sqrt{5}}r_{-1}^1 + \sqrt{3}r_1^2 & 1 + \sqrt{3}r_0^2 \end{bmatrix}$$

\*Erik Thomé, *Multistrange and Charmed Antihyperon-Hyperon Physics for PANDA*  
Ph. D. Thesis, Uppsala University (2012)





## Joint Angular Distribution of the Two Decays

**Spin  $\frac{3}{2}$  hyperons**

Assumptions :  $\alpha_\Omega = 0$ ,  $\beta_\Omega \approx 0$

CP-invariance:  $\beta_\Omega \approx 0$ ,  $\gamma_\Omega \approx 1$   
can be tested by

$$\frac{\beta_\Omega}{\gamma_\Omega} = \frac{\langle \cos \theta_p \sin \phi_p \rangle}{\langle \sin \theta_p \sin \phi_p \rangle}$$

$$\langle (3 \cos \Theta_\Lambda - 1) \sin \phi_p \rangle =$$

$$= \int_0^\pi \int_0^{2\pi} \int_0^\pi \int_0^{2\pi} I(\Theta_\Lambda, \phi_\Lambda, \Theta_p, \phi_p) \times$$

$$\sin \Theta_\Lambda (3 \cos \Theta_\Lambda - 1) \sin \Theta_p \sin \phi_p d\Theta_\Lambda d\phi_\Lambda d\Theta_p d\phi_p =$$

$$= -\frac{3\pi\alpha_\Lambda\gamma_\Omega r_{-1}^1}{20\sqrt{10}}$$

$$\langle (15 \cos \Theta_\Lambda - 1) \sin \phi_p \rangle =$$

$$= \int_0^\pi \int_0^{2\pi} \int_0^\pi \int_0^{2\pi} I(\Theta_\Lambda, \phi_\Lambda, \Theta_p, \phi_p) \times$$

$$\sin \Theta_\Lambda (15 \cos \Theta_\Lambda - 1) \sin \Theta_p \sin \phi_p d\Theta_\Lambda d\phi_\Lambda d\Theta_p d\phi_p =$$

$$= \frac{\sqrt{3}\pi\alpha_\Lambda\gamma_\Omega r_{-1}^3}{2\sqrt{5}}$$

$$\langle \sin \phi_\Lambda \cos \phi_p \rangle =$$

$$= \int_0^\pi \int_0^{2\pi} \int_0^\pi \int_0^{2\pi} I(\Theta_\Lambda, \phi_\Lambda, \Theta_p, \phi_p) \times$$

$$\sin \Theta_\Lambda \sin \Theta_p \sin \phi_\Lambda \cos \phi_p d\Theta_\Lambda d\phi_\Lambda d\Theta_p d\phi_p =$$

$$= -\frac{3\pi^2\alpha_\Lambda\gamma_\Omega r_{-2}^3}{1024}$$

$$\langle \sin \phi_\Lambda \cos \phi_\Lambda \sin \phi_p \rangle =$$

$$= \int_0^\pi \int_0^{2\pi} \int_0^\pi \int_0^{2\pi} I(\Theta_\Lambda, \phi_\Lambda, \Theta_p, \phi_p) \times$$

$$\sin \Theta_\Lambda \sin \Theta_p \sin \phi_\Lambda \cos \phi_\Lambda \sin \phi_p d\Theta_\Lambda d\phi_\Lambda d\Theta_p d\phi_p =$$

$$= -\frac{\pi\alpha_\Lambda\gamma_\Omega}{640} \left( 5\sqrt{6}r_{-3}^3 - 4\sqrt{15}r_{-1}^3 - 3\sqrt{10}r_{-1}^1 \right)$$